

Homework 4

Due November 21, 2000

1. Convert the following FOL sentences to clause form
 - a) $\exists x \forall y [P(x, y) \wedge Q(x, y) \Rightarrow R(x)]$
 - b) $\forall x [\sim \text{Clear}(x) \Rightarrow \exists y \text{On}(y, x)]$
 - c) $\forall x [P(x) \Rightarrow Q(x) \wedge R(x)]$
 - d) $\exists x [\sim(P(x) \wedge Q(x)) \Rightarrow R(x)]$
2. Unify the argument lists of each of the following pairs of opposite literals (i.e., find their most general unifier q)
 - a) $P(f(x))$ and $\sim P(y)$
 - b) $P(x, a, y)$ and $\sim P(z, z, b)$
 - c) $P(x, f(x))$ and $\sim P(a, y)$
3. Explain why the following pairs of opposite literals are not unifiable
 - a) $P(x, x)$ and $\sim P(a, b)$
 - b) $\text{Ancestor}(x, \text{son}(x))$ and $\sim \text{Ancestor}(\text{Bill}, \text{George})$
 - c) $P(f(x), x)$ and $\sim P(y, y)$
4. Use resolution refutation to prove that

$$\exists x [I(x) \wedge \sim R(x)]$$

is a logical consequence of the following set of axioms

$$A1: (\sim R(x), L(x))$$

$$A2: (\sim D(x), \sim L(x))$$

$$A3: (D(\text{sk}_1))$$

$$A4: (I(\text{sk}_1))$$

where sk_1 is a skolem constant

[Hint: Convert the negation of the theorem to clause form first and then try to derive the null clause by resolution.]