

1. **Derivation and Parse Tree:**

Derive the string using leftmost derivation and draw the parse tree for the following grammar.

i) **String:** *abbbaaabbaba*

Grammar:

$S \rightarrow aB \mid bA$

$A \rightarrow a \mid aS \mid bAA$

$B \rightarrow b \mid bS \mid aBB$

ii) **Expression:** $y = \cos(x) - \sin(z) * \log(y)$

Grammar:

$S \rightarrow V = E \mid E$

$V \rightarrow x \mid y \mid z$

$E \rightarrow E + T \mid E - T \mid T$

$T \rightarrow T * F \mid T / F \mid F$

$F \rightarrow (E) \mid V \mid \text{fun}(V)$

$\text{fun} \rightarrow \sin \mid \cos \mid \log$

2. **Ambiguity Check:**

Demonstrate that the following grammar is ambiguous:

$S \rightarrow I$

$I \rightarrow E + E \mid (E) \mid E * E \mid I$

$E \rightarrow a-z \mid 0-9$

The expression you will check with should have a digit in it.

3. **Regular Expression Matching:**

Determine which of the following words are accepted by the given simple regular expressions.

i) $(a+b)a(a+b)(a+b)^*$

a) abbabab

b) baaabba

c) abbaabb

d) aabaab

ii) $(a+b)^*bb(a+b)(a+b)$

a) abababba

b) babbaabb

c) ababbbba

d) bbbabba

4. **Regular Expression Construction:**

Construct a regular expression for the following language:

$L = \{ a^m b^n \mid m * n \text{ is odd} \}$

5. **EBNF to BNF Conversion:**

Convert the following EBNF to BNF:

$S \rightarrow A\{cA\}$

$A \rightarrow a[c]A$