



# CMSC 435/634

## Texture





# Texture Mapping

- Def: mapping a function onto a surface; function can be:
  - 1, 2, or 3D
  - sampled (image) or mathematical function



# Mapped Parameters

- Surface color (Catmull 74)
- Specular reflection (Blinn and Newell 76)
- Normal vector perturbation (Blinn 78)
- Specularity (Blinn 78)
- Transparency (Gardner 85)
- Diffuse Reflection (Miller and Hoffman 84)
- Shadows, displacements, etc (Cook 84)
- Local coord system (Kajiya 85)



# Map Indices

- Surface parameters
- Ray direction
  - reflection/environment mapping
- Surface normal direction
  - diffuse reflection mapping
  - transparency/refraction mapping



# Key Challenges

- Mapping function determination
- Resolution issues
- Texture design/capture



# Mapping Functions

- Standard projecting functions
  - planar
  - cylindrical
  - spherical
- Mechanism
  - Two-stage mapping
  - Reverse projection
- Arbitrary



# Two-stage Mapping

- S-mapping
  - map to simple 3D shape
  - intermediate surfs: plane, cylinder, cube, sphere
- O-mapping
  - map 3D texture onto surface
  - map entities: reflected view ray, surface normal, line through centroid, intermediate surface normal

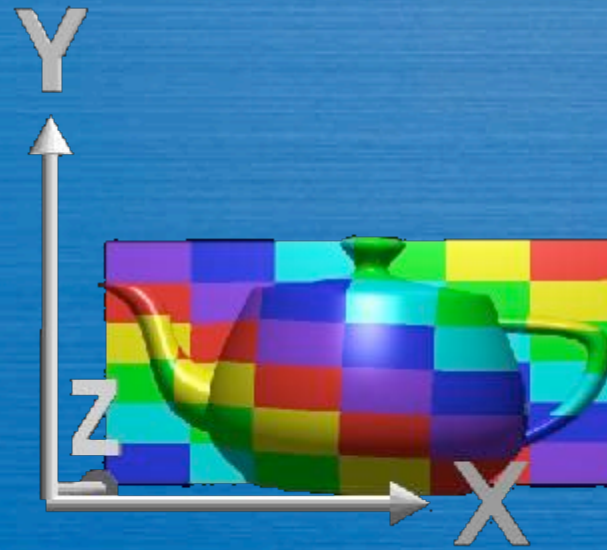


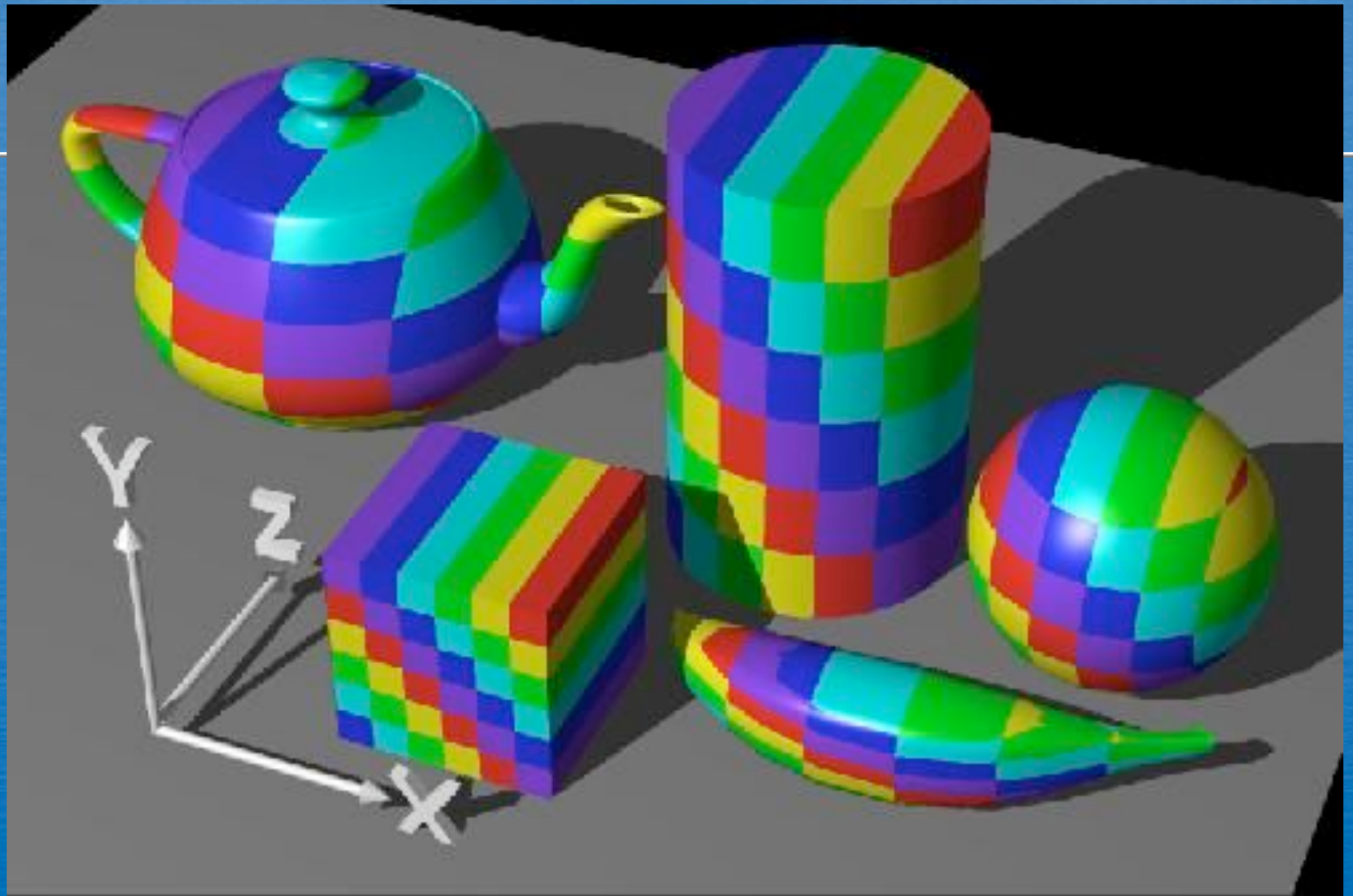
# Planar Mapping

- For xy aligned plane

$$(u, v) = \left( \frac{x - x_1}{x_r - x_1}, \frac{y - y_1}{y_r - y_1} \right)$$

- Reverse projection

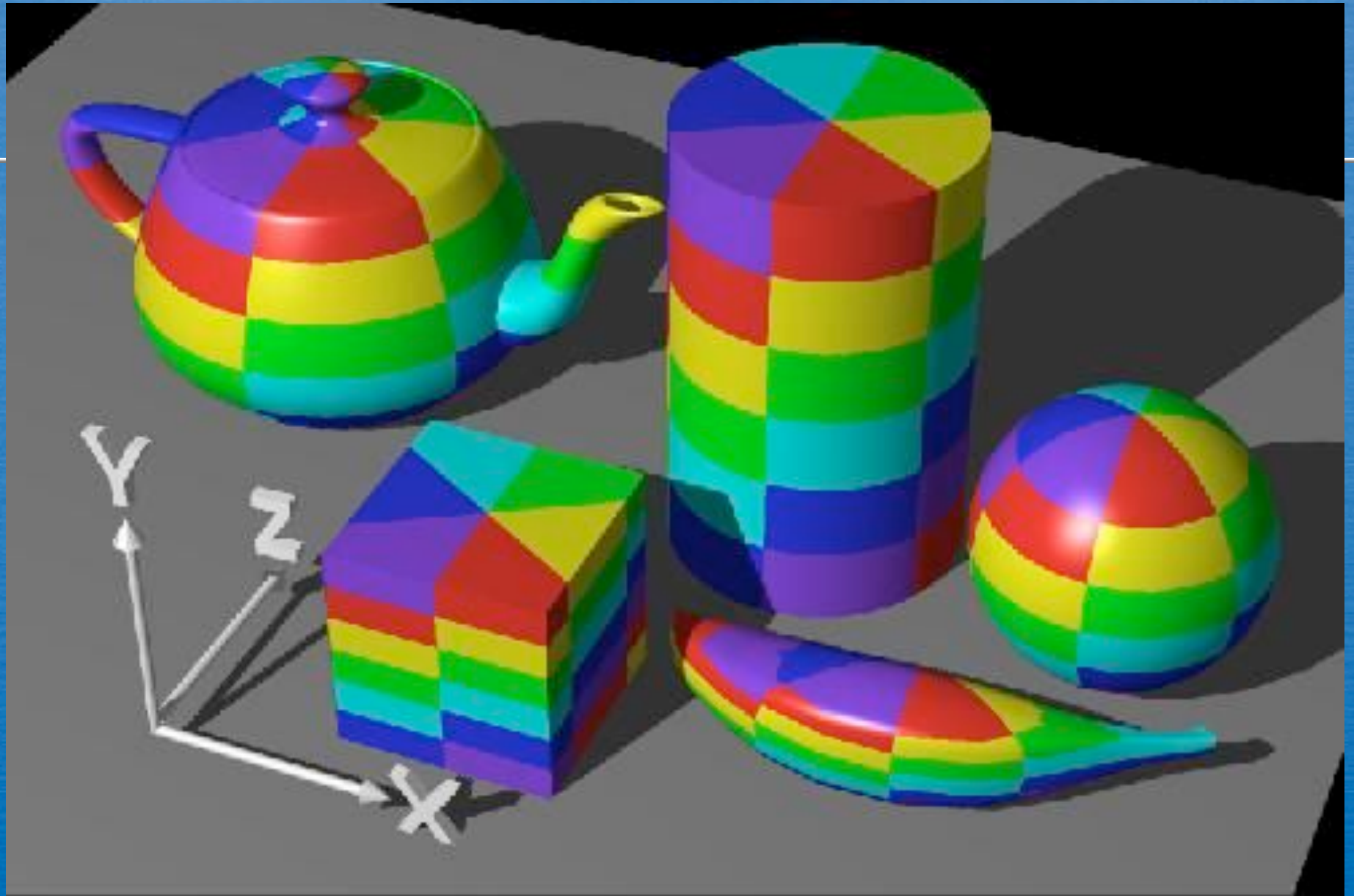




# Cylindrical Mapping

- For cylinder with point  
 $(r \cos\theta, r \sin\theta, h z)$
- Texture coords  
 $(u,v) = (\theta/2\pi, z)$

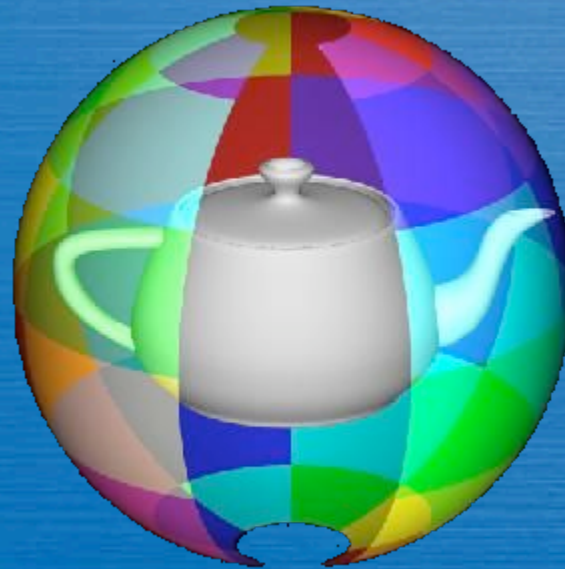


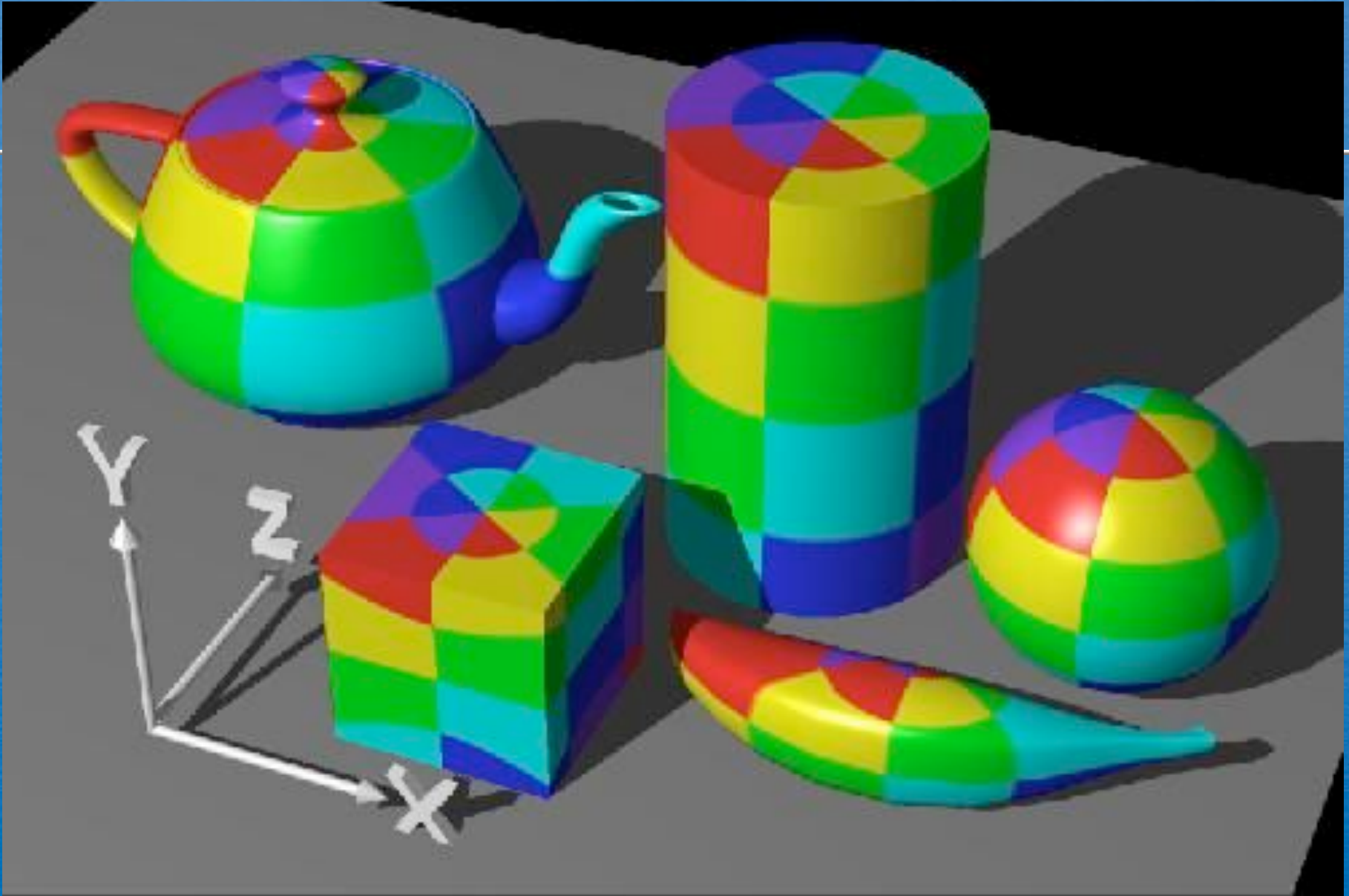


# Spherical Mapping

- For sphere with point  
( $r \cos\theta \sin\phi$ ,  $r \sin\theta \sin\phi$ ,  $r \cos\phi$ )
- Texture coords

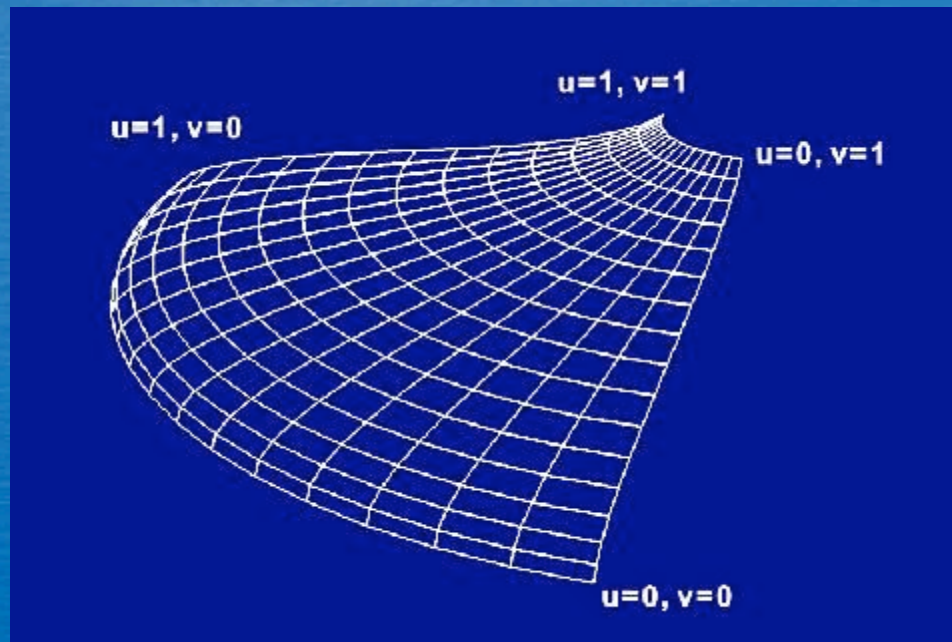
$$(u, v) = \left( \frac{\theta}{\pi/2}, \frac{\pi/2 - \phi}{\pi/4} \right)$$

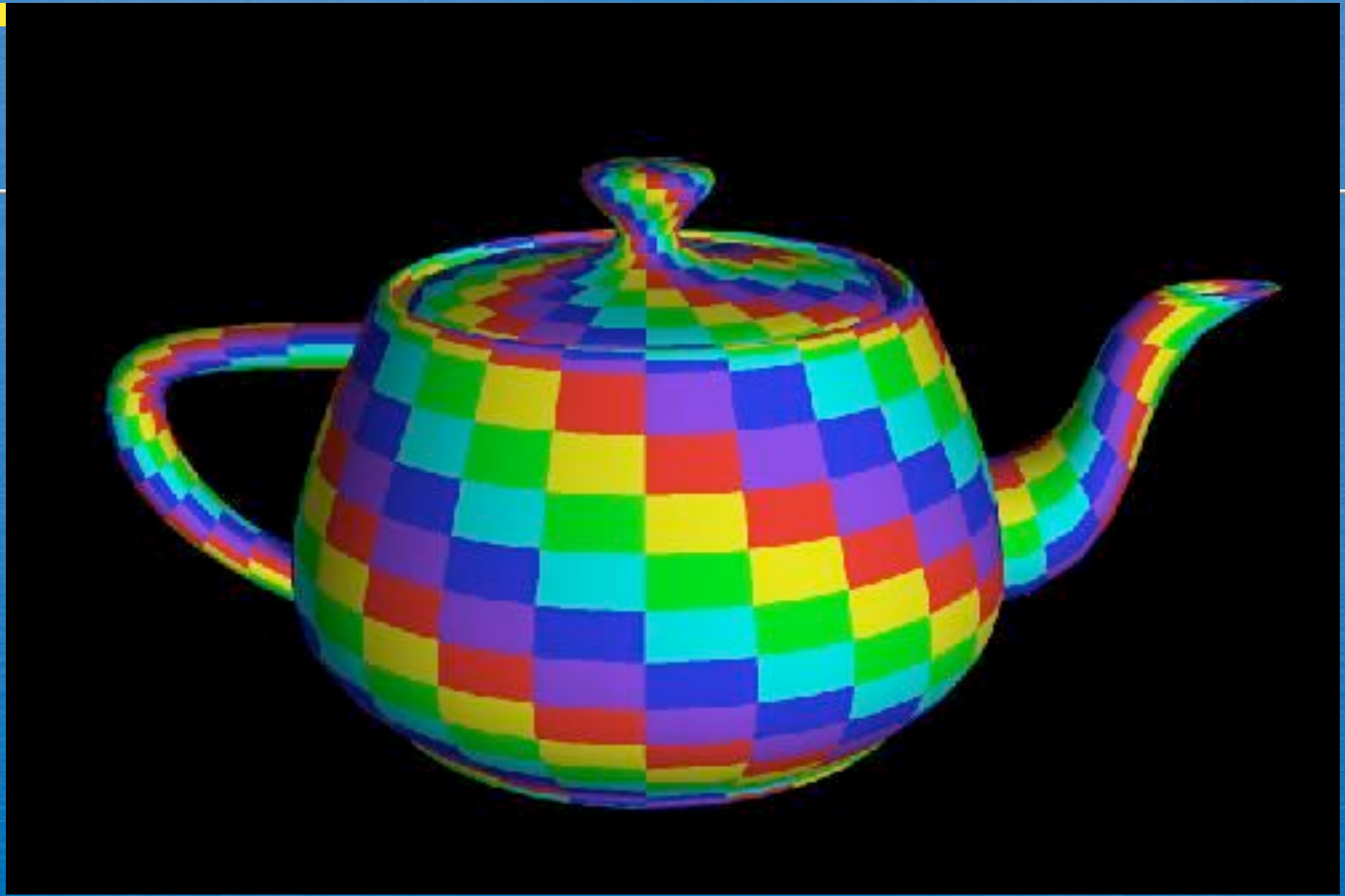




# Mapping onto Parametric Patches

- Use scaled surface  $u, v$  parameters for texture  $u, v$



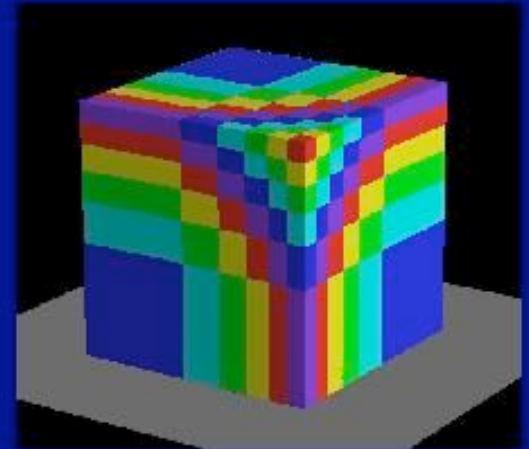
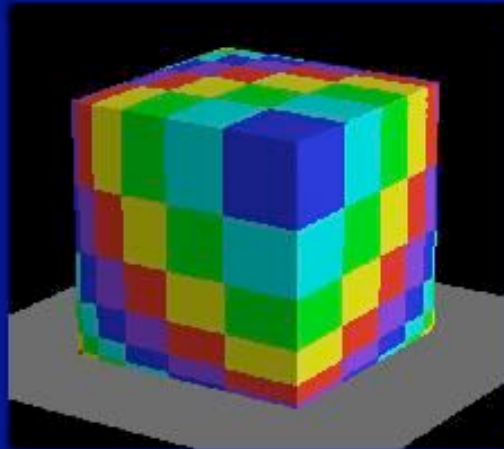
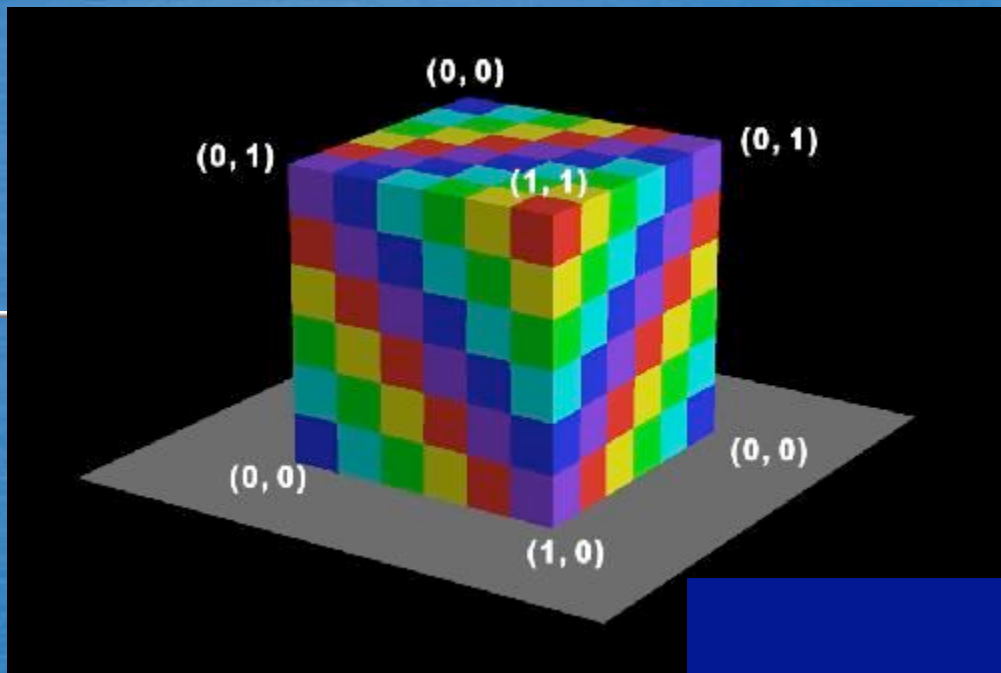






# Mapping onto Polygons

- Like parametric surfaces, but use explicit vertex texture coordinates
- Screen-space Interpolation
  - Interpolate  $u, v$
  - Nonlinearity and errors from lack of rotational invariance
  - use small polygons to minimize artifacts
- Correct solution: per-pixel projection
  - Interpolate  $(u/w, v/w, 1/w)$ ; divide to get pixel  $(u, v)$



# Bump Mapping

- Perturb surface normals to simulate shape variations







Bump mapping

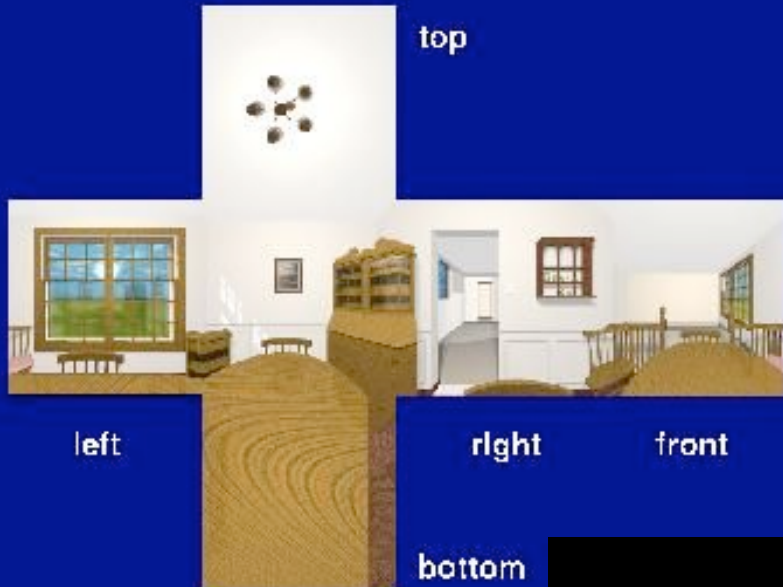


Displacement Mapping



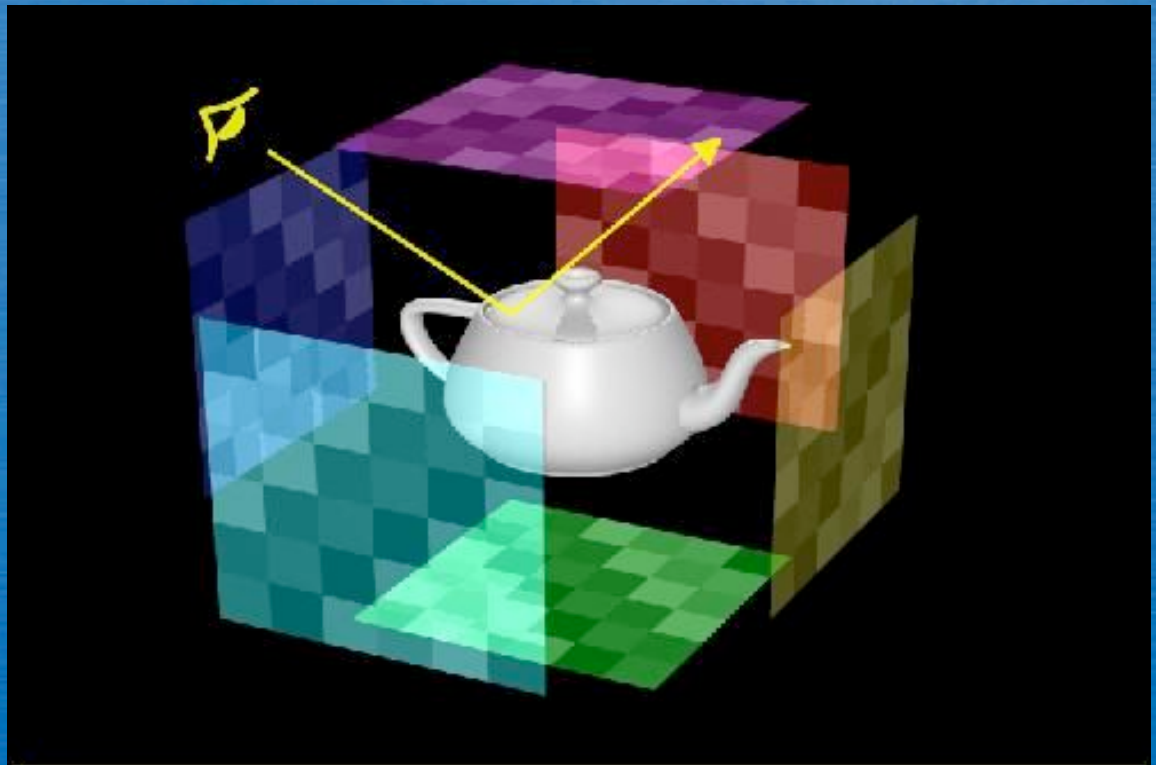
# Reflection Mapping

- Look up reflections on an object from a map simulating surrounding environment



# Environment Mapping

- Surround scene with maps simulating surrounding detail







Ray tracing

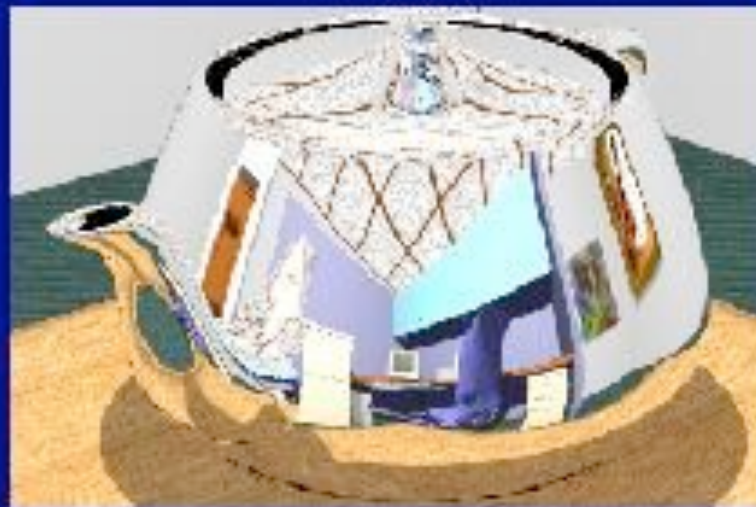
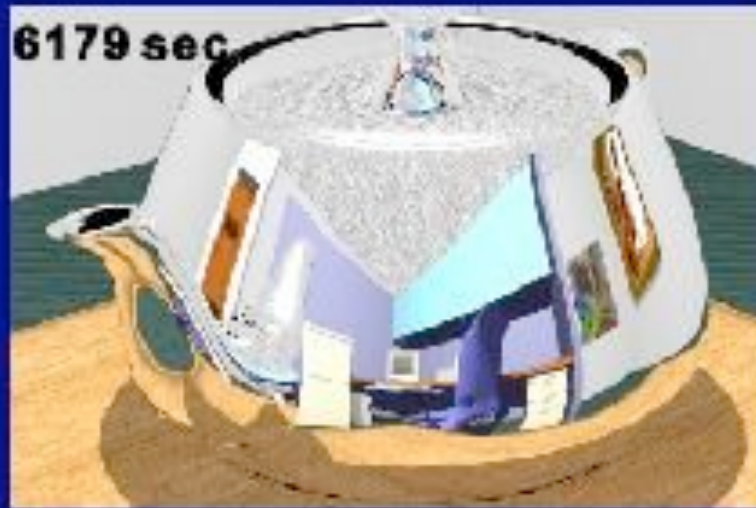


Environment Mapping



Ray tracing

Environment mapping



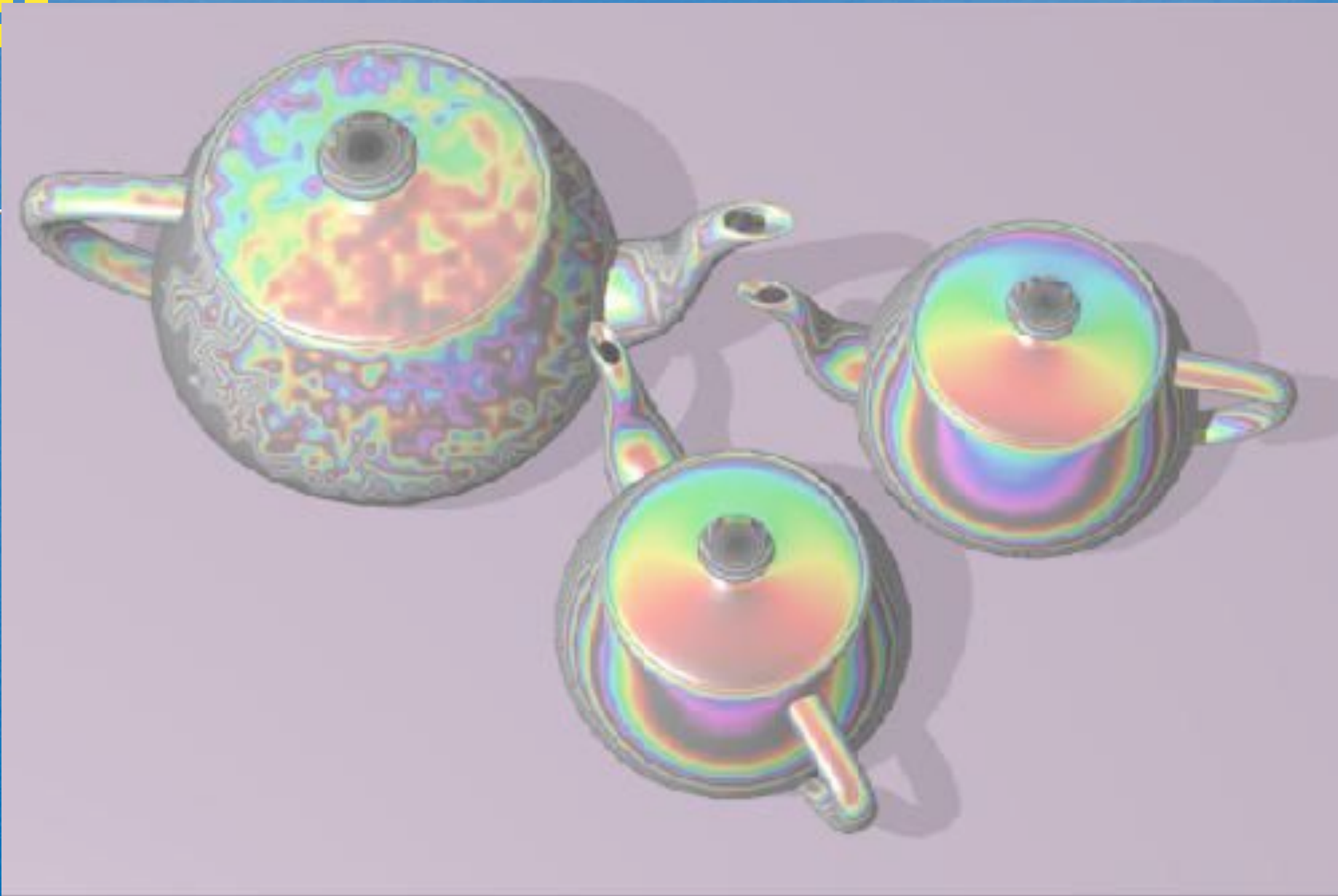
Ray tracing

Environment Mapping



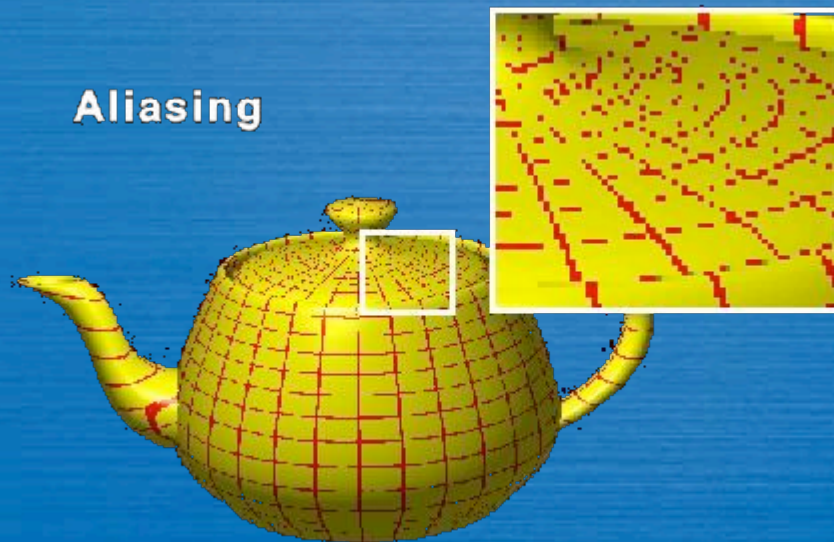
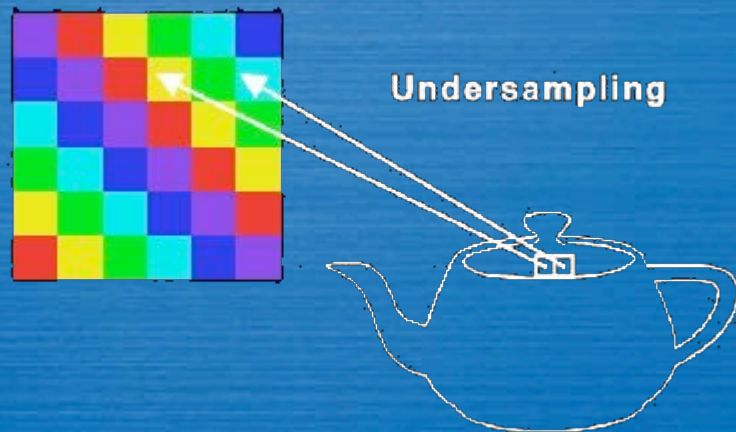
# Refraction Mapping

- Perturb refraction rays through transparent surface by disruption of surface normal



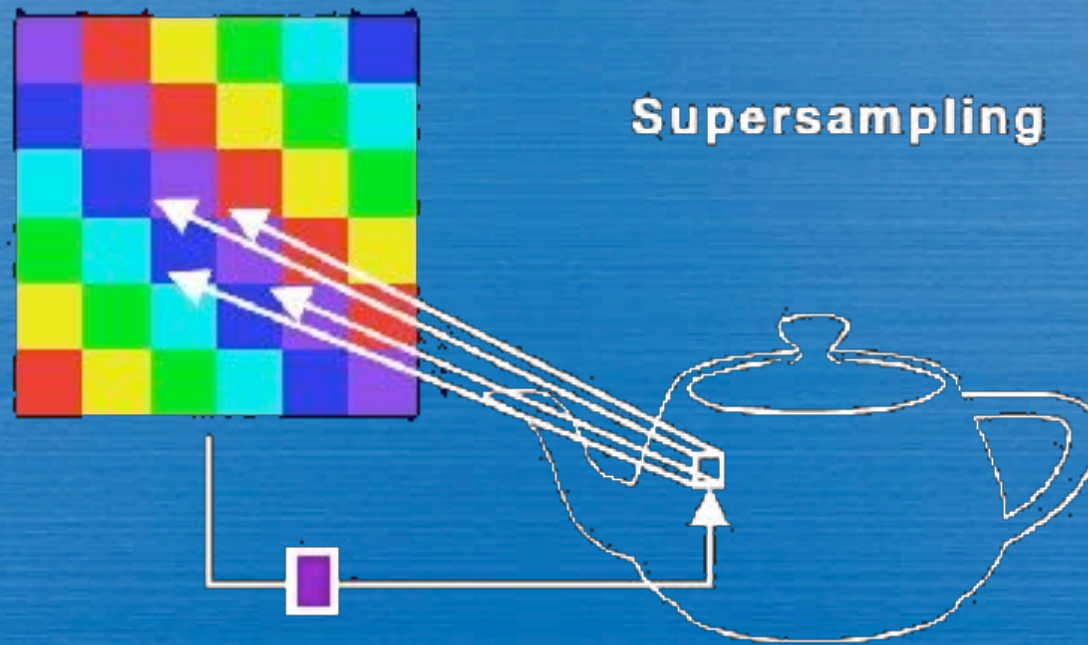
# Texture Aliasing

- Undersampling of texture map leads to texture aliasing
- Oversampling can show limited texture resolution



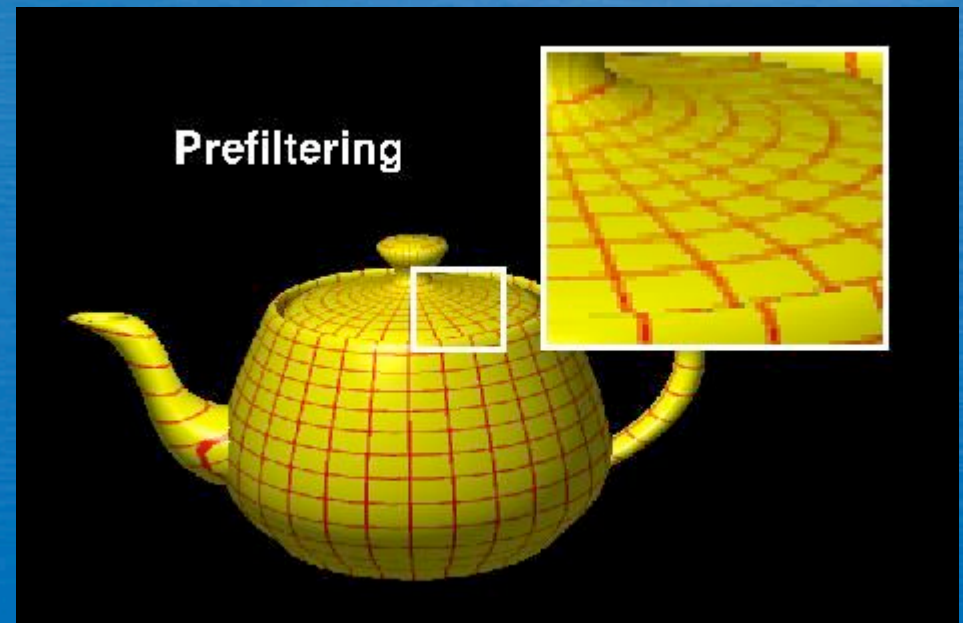
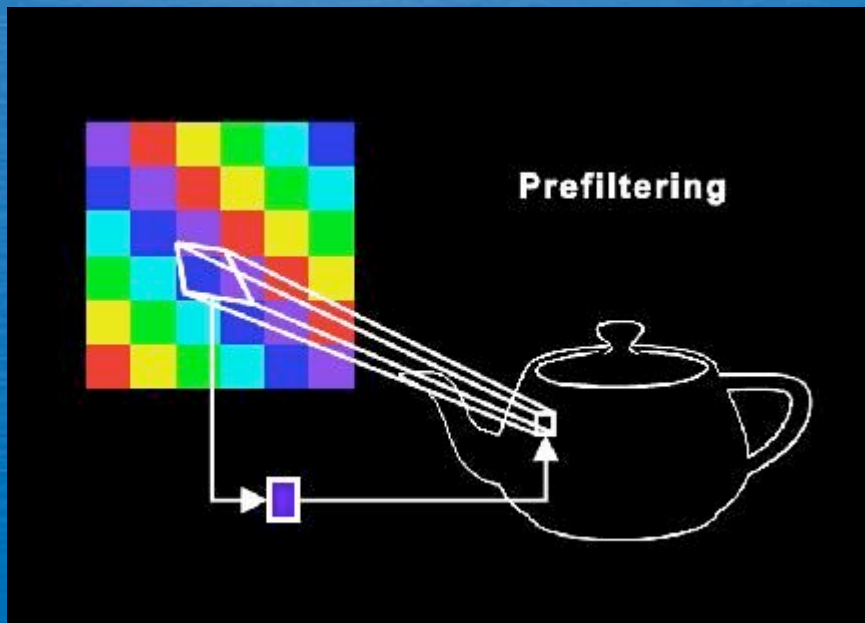
# Supersampling

- Sample texture multiple times per pixel and reconstruct



# Filtering

- Basic method (Catmull 78)
  - Project pixel pgon onto texture map
  - Average color over projected area







# Filtering Types

- Direct Convolution
  - average multiple samples from texture (usually selected in texture space)
- Prefiltering
  - construct multi-resolution copies of texture
- Fourier filtering
  - low pass filter texture in frequency space

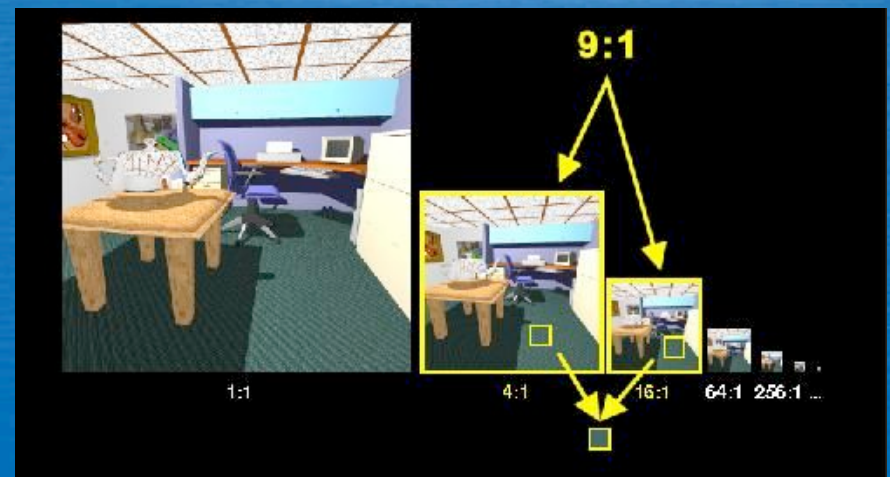
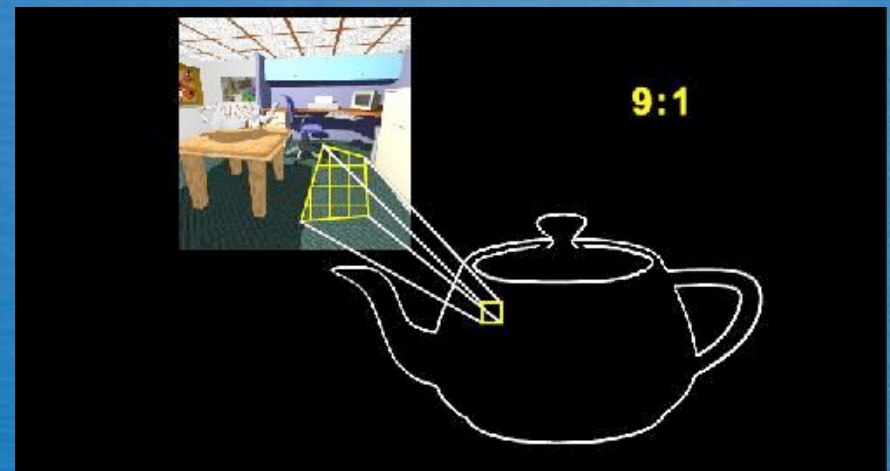
# Mipmapping

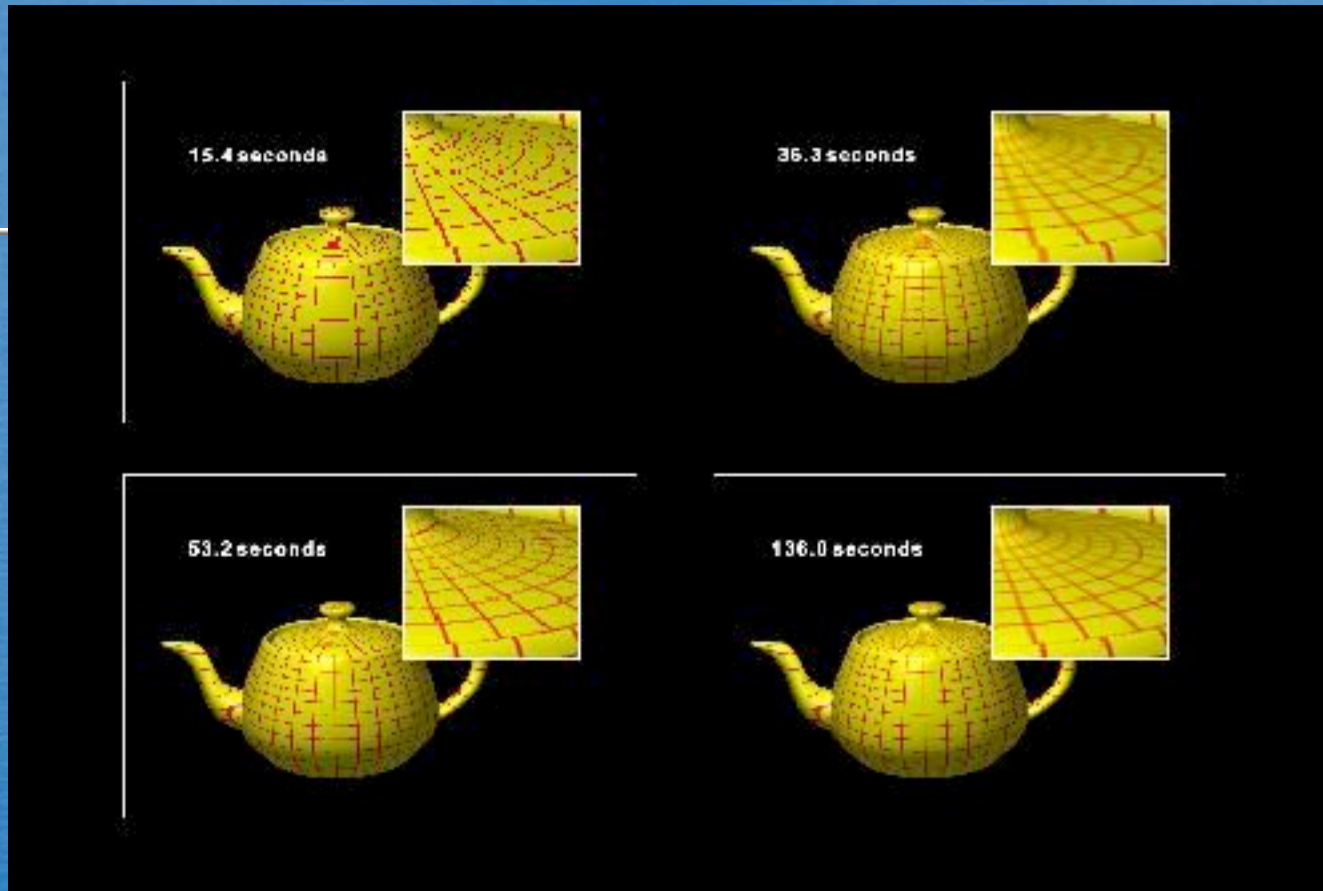
- Precalculate filtered maps at a range of resolutions (Williams 83)
- Higher memory requirements



# Mipmapping Process

- Compute pixel area in mipmap
- Average from two closest maps





Anti-aliasing: none, mipmapped, supersampled,  
supersampling and mipmapping