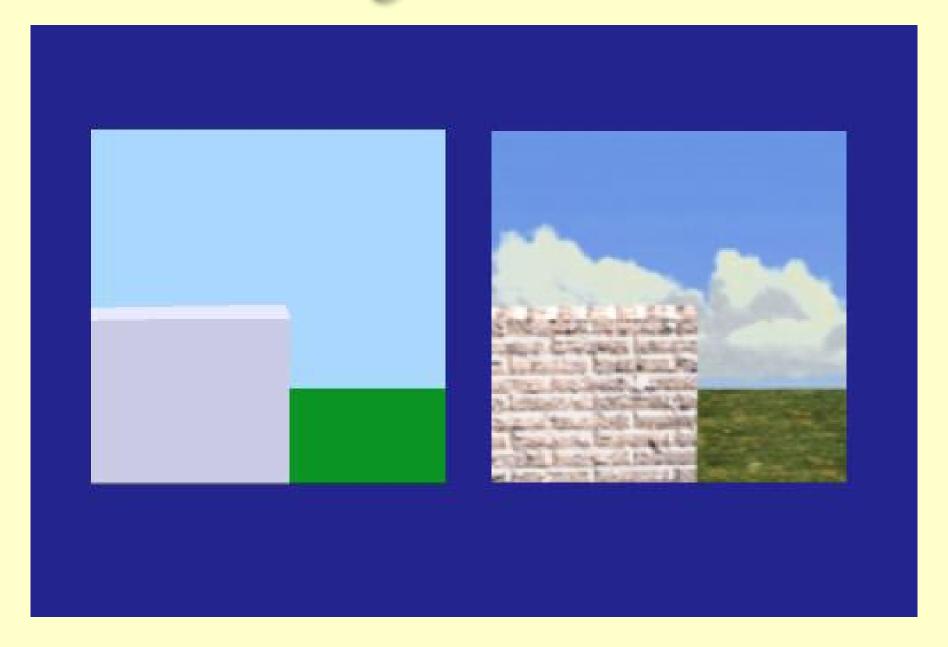
#### CMSC 435/634

#### **Texture**

## Texturing Adds Richness



#### Texture Mapping

Mapping a function onto a surface Function can be

- 1D, 2D or 3D
- Sampled (i.e. an image) or a mathematical function

#### Mapped Parameters

- Surface color (Catmull 74)
- Specular reflection (Blinn and Newell 76)
- Normal vector perturbation (Blinn 78)
- Specularity (Blinn 78)
- Transparency (Gardner 85)
- Diffuse Reflection (Miller and Hoffman 84)
- Shadows, displacements, etc (Cook 84)
- Local coord system (Kajiya 85)

#### Map Indices

#### Surface parameters

- Position
- Surface parameterization
- Manually defined texture coordinates

#### Ray direction

reflection/environment mapping

#### Surface normal direction

- diffuse reflection mapping
- transparency/refraction mapping

## Key Challenges

Mapping function determination Resolution issues Texture design/capture

## Mapping Functions

#### Standard projecting functions

- planar
- cylindrical
- spherical

#### Mechanism

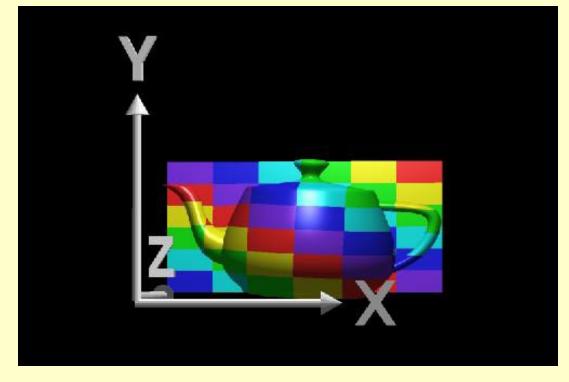
- Two-stage mapping
- Reverse projection

#### Planar Mapping

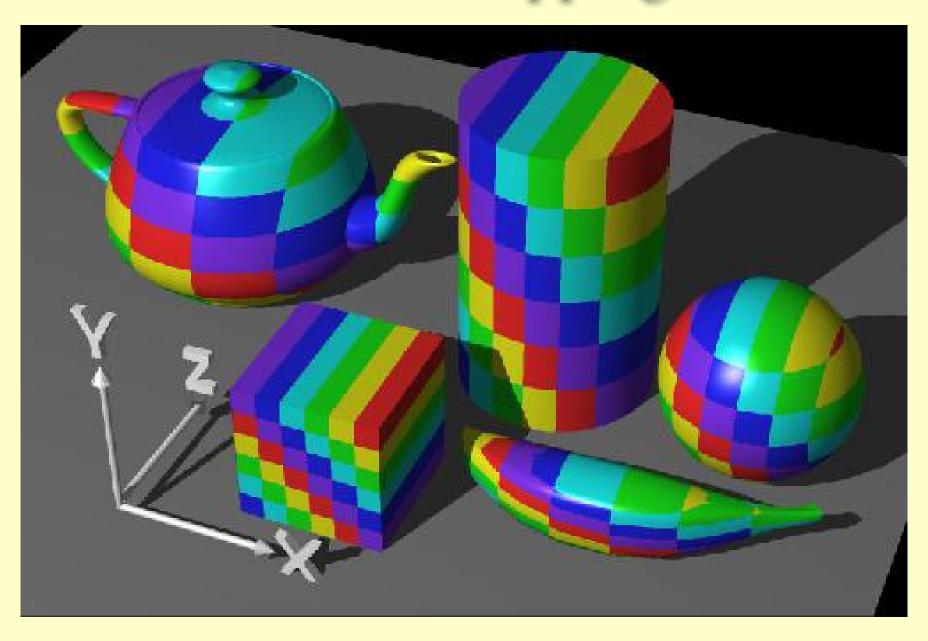
Parallel Projection of Texture

Reverse Map Position to Texture Coordinate

$$(u,v) = \left(\frac{x-x_1}{x_r-x_1}, \frac{y-y_1}{y_r-y_1}\right)$$



# Planar Mapping

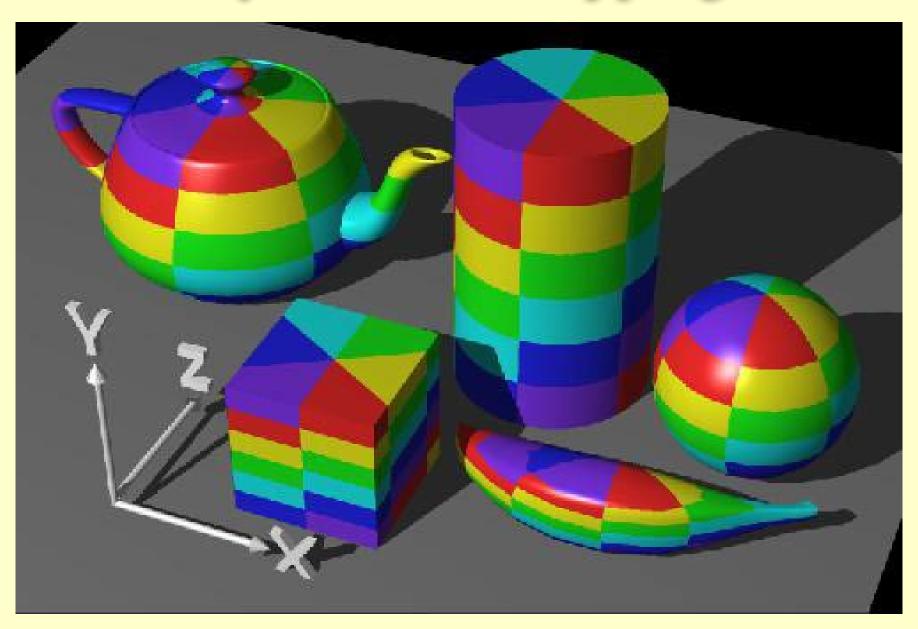


## Cylindrical Mapping

For cylinder with point  $(r\sin\theta, r\cos\theta, h\ z)$ Texture coordinate  $(u,v)=(\theta/2\pi,z)$ 



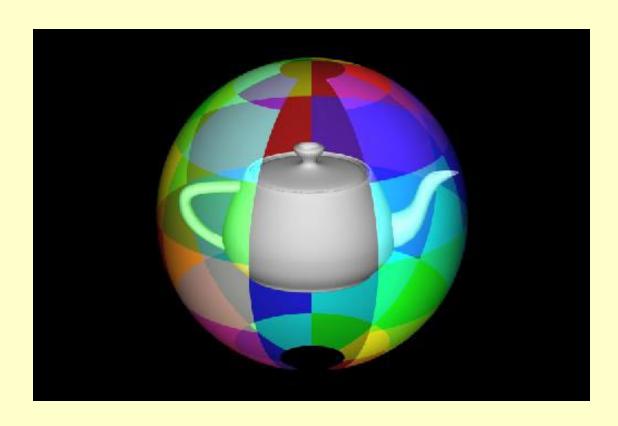
# Cylindrical Mapping



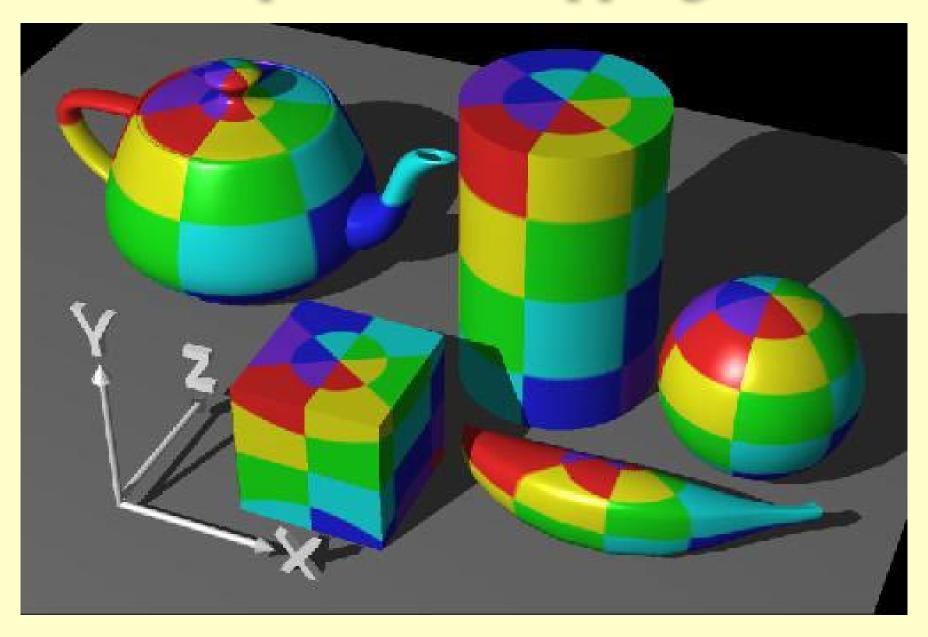
### Spherical Mapping

Sphere point  $(r\cos\theta\sin\phi, r\sin\theta\sin\phi, r\cos\phi)$ 

Texture coordinate 
$$(u,v) = \left(\frac{\theta}{\pi/2}, \frac{\pi/2 - \phi}{\pi/4}\right)$$



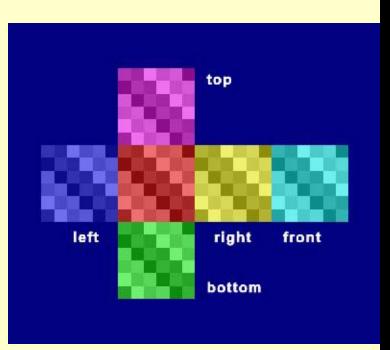
# Spherical Mapping

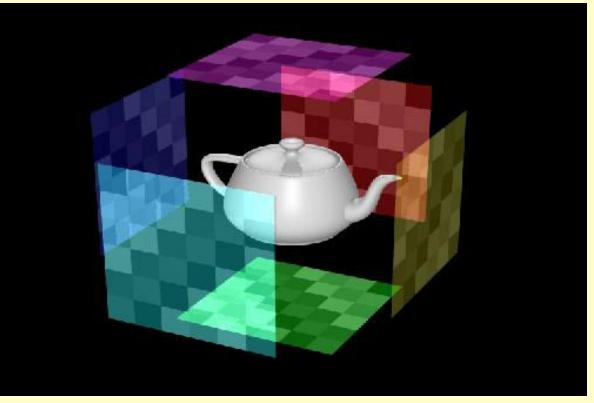


### **Environment Mapping**

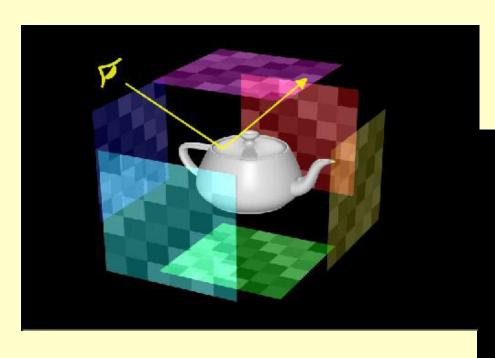
Map vector direction to texture coordinates

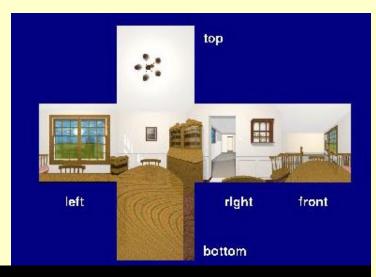
- Any mapping of *vector* to *texture* will work
- Cube map uses texture on six faces of cube





Map based on reflection direction





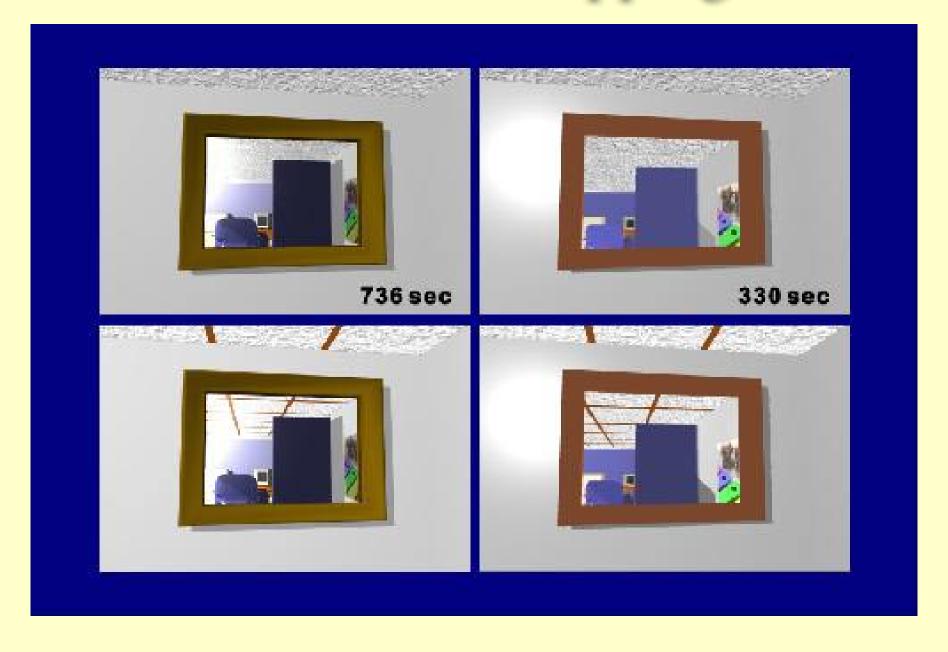


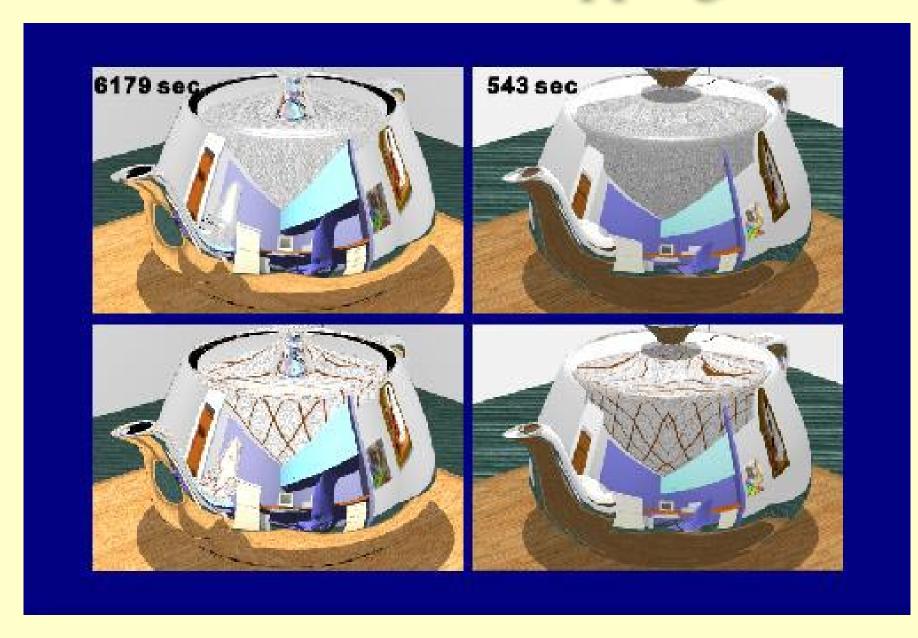


Ray Tracing



Reflection Mapping





#### Cube Environment Map

Choose cube face from largest vector component

$+x:+x>\pm y,\pm z$	$+y:+y>\pm z, \pm x$	$+z:+z>\pm x, \pm y$
$-x:-x>\pm y,\pm z$	$-y:-y>\pm z, \pm x$	$-z:-z>\pm x,\pm y$

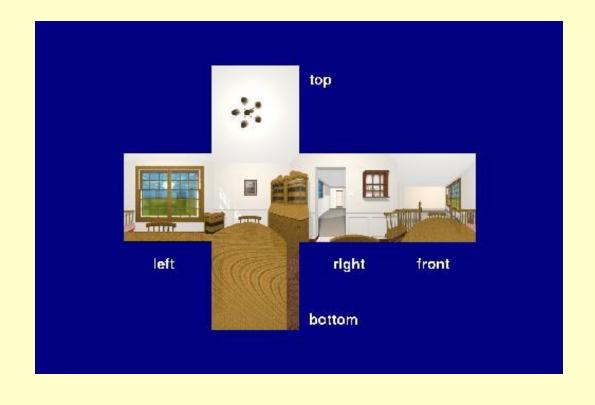
Perspective project onto face

+x: y/x, z/x

Transform resulting

—1 to 1 into texture

space



### Sphere Environment Map

#### Texture = reflection from shiny sphere

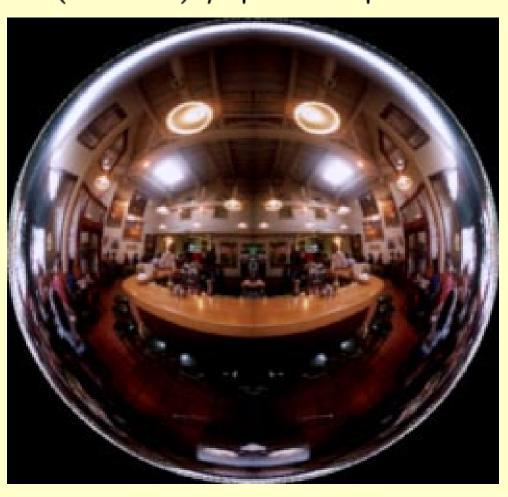
- Normal for reflection =  $\hat{\mathbf{h}} = (\hat{\mathbf{v}} + \hat{\mathbf{r}}) / |\hat{\mathbf{v}} + \hat{\mathbf{r}}|$
- Transform x and y components to texture coord

#### Advantages

- Easy to aquire
- Easy to use

#### Disadvantages

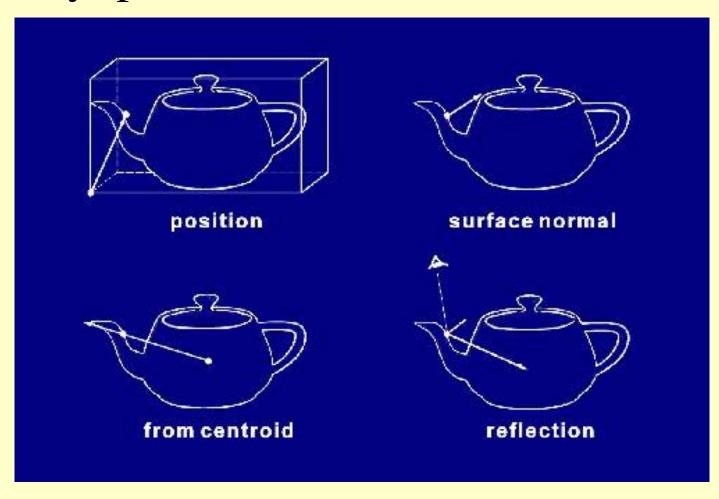
- Fixed view
- Poor sampling near edge



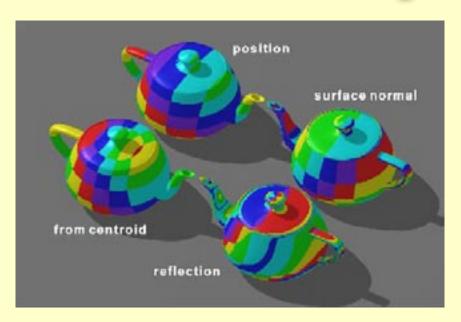
#### Map Entity vs. Map Shape

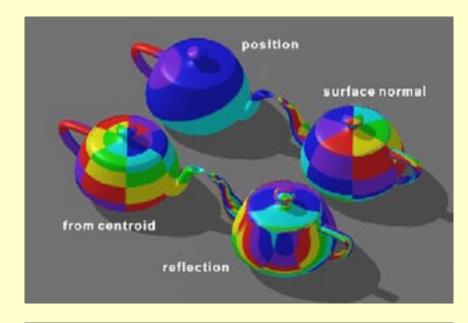
Map shape: sphere, cylinder, cube, plane, ...

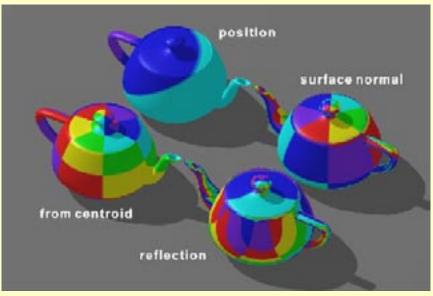
Map entity: position, normal, reflection vector, ...

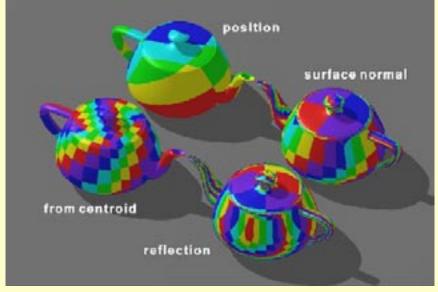


## Map Entities



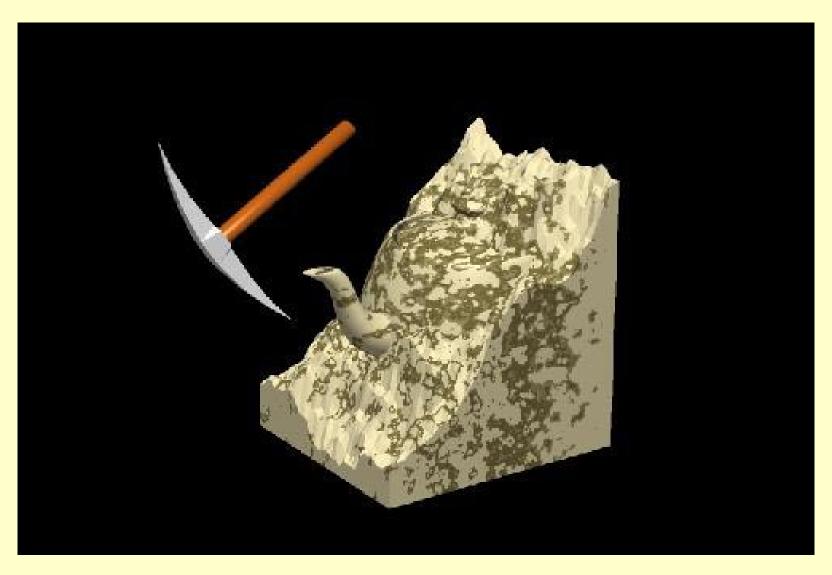






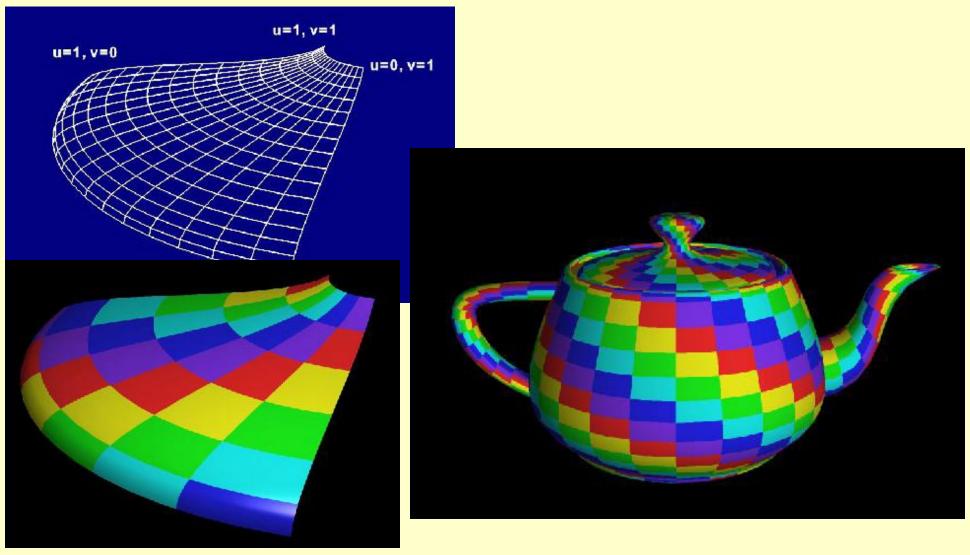
### Solid/3D texture

#### 3D Position in 3D volume texture



#### Parametric Patches

Use scaled surface u,v for texture u,v



## Mapping onto Polygons

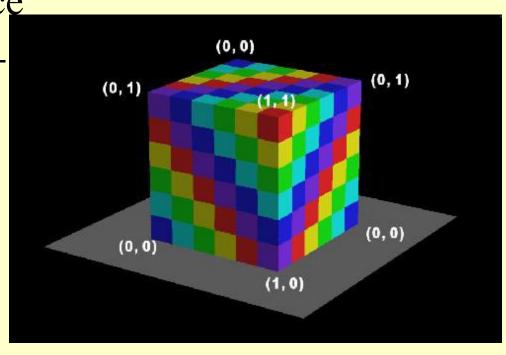
Like parametric surfaces, but use explicit vertex texture coords

#### Interpolation issues

 screen space interp results in errors from nonlinearity and lack of rotational invariance

 use small polygons to minimize artifacts

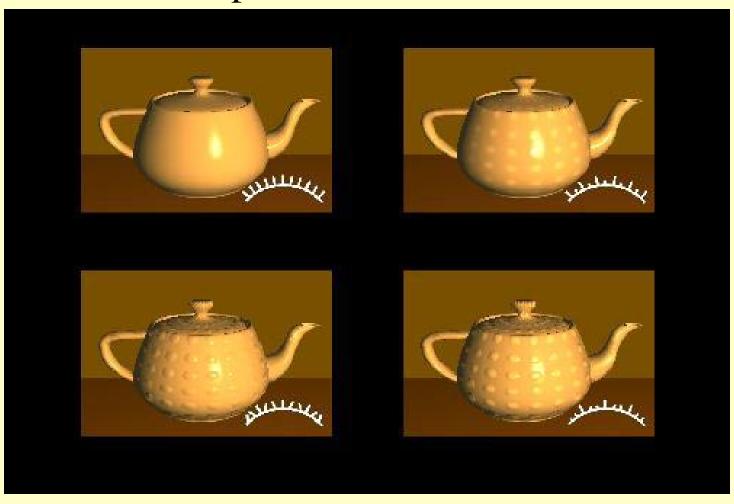
Correct solution: actual projection at each pixel



## **Bump Mapping**

#### Purterb surface normal

• Simulate minor shape variations



# Bump Mapping



### Displacement Mapping

Actually perturb surface



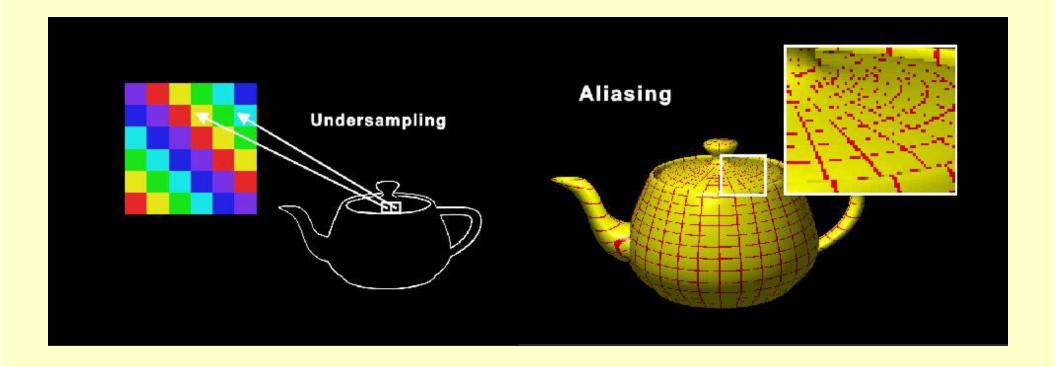
#### Texture Sampling

Oversampling: shows limited texture resolution

Magnification

Undersampling: aliasing

Minification

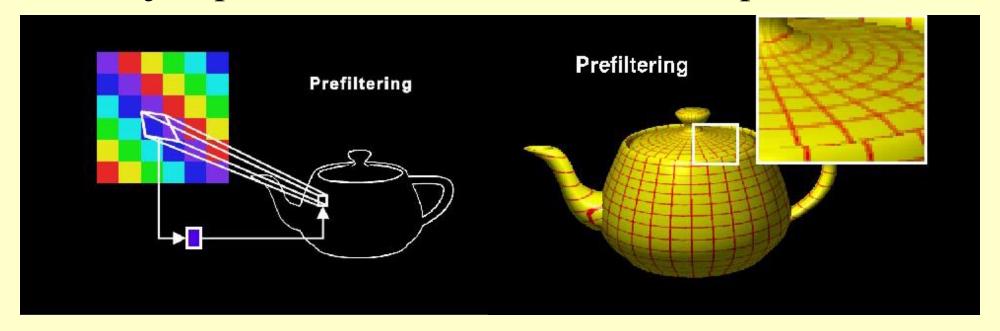


#### Texture Filtering

Similar to pixel antialiasing

**BUT** texture is known in advance

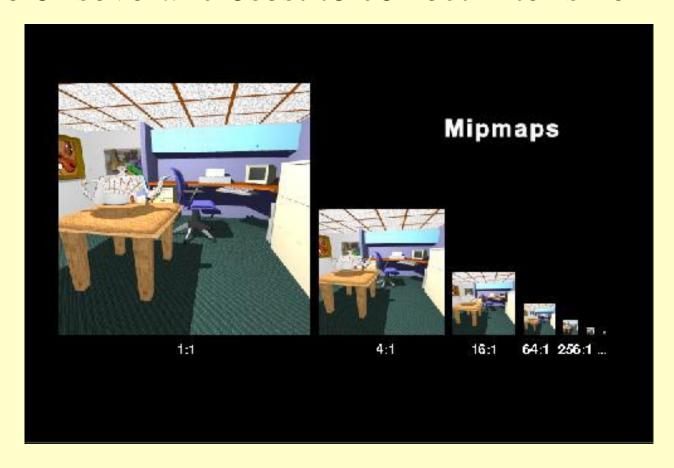
- Can improve overall antialiasing by filtering texture first
- Do faster and better by using prefiltering
  - Project pixel to texture, filter in texture space



#### Texture Prefiltering

#### MIPMap (Williams 78)

- Pre-filter at a sequence of resolutions
- Use one or several closest to correct filter size



#### Mipmap Reconstruction

#### Trilinear filtering:

- Find area in texture
- Average texels within two closest mipmaps
- Average between two closest mipmaps



#### Texture + Pixel Antialiasing

