





CMSC 461, Database Management Systems Spring 2018

Lecture 13 - Chapter 8 Relational Database Design Part 3

These slides are based on "Database System Concepts" 6th edition book and are a modified version of the slides which accompany the book

(http://codex.cs.yale.edu/avi/db-book/db6/slide-dir/index.html), in addition to the 2009/2012 CMSC 461 slides by Dr. Kalpakis

Logistics

• Midterm 3/14/2018

Lecture Outline

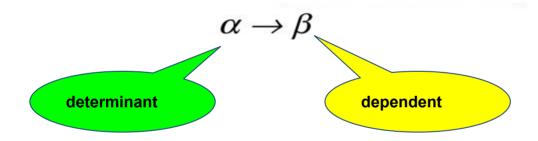
- Functional Dependencies Review
- BCNF Decomposition
- Database Design Process
- Midterm Review

We represent constraints by using keys

- super keys
- primary keys
- candidate keys

We can also represent constraints using functional dependencies

- A functional dependency is a relationship between two attributes, where β is functionally dependent on α
- α is usually the primary key
- For every valid instance of α , that value uniquely determines the value of β .



What are the dependencies in Table Foo?

| Table Foo: | | | | |
|------------|----|----|----|----|
| Α | В | С | D | Е |
| a1 | b1 | с1 | d1 | e1 |
| a2 | b1 | c2 | d2 | e1 |
| a3 | b2 | с1 | d1 | e1 |
| a4 | b2 | c2 | d2 | e1 |

Can we say this:

$$A \rightarrow B$$
, $A \rightarrow C$, $A \rightarrow D$, $A \rightarrow E$

| Table Foo: | | | | |
|------------|----|----|----|----|
| Α | В | С | D | Е |
| a1 | b1 | с1 | d1 | e1 |
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| a3 | b2 | с1 | d1 | e1 |
| a4 | b2 | c2 | d2 | e1 |

If we can say this:

$$A \rightarrow B$$
, $A \rightarrow C$, $A \rightarrow D$, $A \rightarrow E$

Then we can say:

 $A \rightarrow BC$ (or any other subset of ABCDE)

| Table Foo: | | | | |
|------------|----|----|----|----|
| Α | В | С | D | Е |
| a1 | b1 | с1 | d1 | e1 |
| a2 | b1 | c2 | d2 | e1 |
| а3 | b2 | с1 | d1 | e1 |
| a4 | b2 | c2 | d2 | e1 |

We can summarize this as A →BCDE

| Table Foo: | | | | |
|------------|----|----|----|----|
| Α | В | С | D | Е |
| a1 | b1 | с1 | d1 | e1 |
| a2 | b1 | c2 | d2 | e1 |
| a3 | b2 | с1 | d1 | e1 |
| a4 | b2 | c2 | d2 | e1 |

Other dependencies we can observe?

| Table Foo: | | | | |
|------------|----|----|----|----|
| Α | В | С | D | Е |
| a1 | b1 | с1 | d1 | e1 |
| a2 | b1 | c2 | d2 | e1 |
| а3 | b2 | с1 | d1 | e1 |
| a4 | b2 | c2 | d2 | e1 |

Functional Dependency Theory

We now consider the formal theory that tells us which functional dependencies are implied logically by a given set of functional dependencies.

Closure of a Set of Functional Dependencies

- Given a set F of functional dependencies, there are certain other functional dependencies that are logically implied by F
 - For example:
 Given a schema r(A,B,C)
 If A → B and B → C
 - then we can infer that A → C
- The set of all functional dependencies logically implied by F is the closure of F
- We denote the closure of F by F⁺
- F⁺ is a superset of F

Closure of a Set of Functional Dependencies

 We can find F⁺, the closure of F, by repeatedly applying

Armstrong's Axioms:

- if $\beta \subseteq \alpha$, then $\alpha \to \beta$ (reflexivity)
- if $\alpha \to \beta$, then $\gamma \alpha \to \gamma \beta$ (augmentation)
- if $\alpha \to \beta$, and $\beta \to \gamma$, then $\alpha \to \gamma$ (transitivity)
- These rules are
 - sound (generate only functional dependencies that actually hold), and
 - complete (generate all functional dependencies that hold).

Computing F+

To compute the closure of a set of functional dependencies F:

```
repeat

for each functional dependency f in F+
   apply reflexivity and augmentation rules on f
   add the resulting functional dependencies to F+

for each pair of functional dependencies f_1 and f_2 in F+
   if f_1 and f_2 can be combined using transitivity

then add the resulting functional dependency to F+

until F+ does not change any further
```

Closure of a set of Functional Dependencies

- Additional rules:
 - If $\alpha \to \beta$ holds and $\alpha \to \gamma$ holds, then $\alpha \to \beta$ γ holds (union)
 - If $\alpha \to \beta \gamma$ holds, then $\alpha \to \beta$ holds and $\alpha \to \gamma$ holds (decomposition)
 - If α → β holds and γ β → δ holds, then α γ
 → δ holds (pseudotransitivity)
 - The above rules can be inferred from Armstrong's axioms.

Closure of a set of Functional Dependencies Example

- R = (A, B, C, Ḡ, H, I)
 F = { A → B
 A → C
 CG → H
 CG → I
 B → H}
- some members of F⁺
 - $-A \rightarrow H$
 - by transitivity from $A \rightarrow B$ and $B \rightarrow H$
 - $-AG \rightarrow I$
 - by augmenting A → C with G, to get AG → CG
 and then transitivity with CG → I
 - CG → HI
 - by union rule, since $CG \rightarrow H$ and $CG \rightarrow I$, implies $CG \rightarrow HI$

Closure of Attribute Sets

- Given a set of attributes α , define the *closure* of α under F (denoted by α +) as the set of attributes that are functionally determined by α under F
- Algorithm to compute α +, the closure of α under F

```
result := \alpha;

while (changes to result) do

for each \beta \to \gamma in F do

begin

if \beta \subseteq result then result := result \cup \gamma

end
```

Closure of Attribute Sets Example

```
• R = (A, B, C, G, H, I)

• F = \{A \rightarrow B \\ A \rightarrow C \\ CG \rightarrow H \\ CG \rightarrow I \\ B \rightarrow H\}

• (AG)^+

1.result = AG

2.result = ABCG (A \rightarrow C \text{ and } A \rightarrow B)

3.result = ABCGH (CG \rightarrow H \text{ and } CG \subseteq AGBC)

4.result = ABCGHI (CG \rightarrow I \text{ and } CG \subseteq AGBCH)
```

Closure of Attribute Sets Uses

There are several uses of the attribute closure algorithm:

- Testing for superkey:
 - To test if α is a superkey, we compute α^+ , and check if α^+ contains all attributes of R.
- Testing functional dependencies
 - To check if a functional dependency α → β holds (or, in other words, is in F+), just check if β ⊆ α+.
 - That is, we compute α+ by using attribute closure, and then check if it contains β.
 - Is a simple and cheap test, and very useful
- Computing closure of F
 - For each $\gamma \subseteq R$, we find the closure γ^+ , and for each $S \subseteq \gamma^+$, we output a functional dependency $\gamma \to S$.

Closure of Attribute Sets Examples

- R = (name,color,category,department,price)
- F = {name → color category → department color,category → price}

You find:

- name+
- {name,category}+
- {color}+

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Lossless-join Decomposition

• For the case of $R = (R_1, R_2)$, we require that for all possible relations r on schema R $r = \prod_{R_1} (\kappa) \prod_{R_2} (r)$

 A decomposition of R into R₁ and R₂ is lossless join if at least one of the following dependencies is in F⁺:

- $\begin{array}{ccc}
 & R_1 \cap R_2 \rightarrow R_1 \\
 & R_1 \cap R_2 \rightarrow R_2
 \end{array}$
- The above functional dependencies are a sufficient condition for lossless join decomposition; the dependencies are a necessary condition only if all constraints are functional dependencies

Example

•
$$R = (A, B, C)$$

 $F = \{A \rightarrow B, B \rightarrow C\}$

- Can be decomposed in two different ways
- $R_1 = (A, B), R_2 = (B, C)$
 - Lossless-join decomposition:

$$R_1 \cap R_2 = \{B\} \text{ and } B \rightarrow BC$$

- Dependency preserving
- $R_1 = (A, B), R_2 = (A, C)$
 - Lossless-join decomposition:

$$R_1 \cap R_2 = \{A\} \text{ and } A \rightarrow AB$$

Not dependency preserving
 (cannot check B → C without computing R₁ ⋈ R₂)

Dependency Preservation

- Let F_i be the set of dependencies F + that include only attributes in R_i.
 - A decomposition is dependency preserving, if $(F_1 \cup F_2 \cup ... \cup F_n)^+ = F^+$
 - If it is not, then checking updates for violation of functional dependencies may require computing joins, which is expensive.

Testing for Dependency Preservation

- To check if a dependency $\alpha \to \beta$ is preserved in a decomposition of R into $R_1, R_2, ..., R_n$ we apply the following test (with attribute closure done with respect to F)
 - result = α while (changes to result) do for each R_i in the decomposition $t = (result \cap R_i)^+ \cap R_i$ result = result $\cup t$
 - If result contains all attributes in β , then the functional dependency
 - $\alpha \rightarrow \beta$ is preserved.

Testing for Dependency Preservation

- We apply the test on all dependencies in F to check if a decomposition is dependency preserving
- This procedure takes polynomial time, instead of the exponential time required to compute F^+ and $(F_1 \cup F_2 \cup \ldots \cup F_n)^+$

Example

•
$$R = (A, B, C)$$

 $F = \{A \rightarrow B \}$
 $B \rightarrow C\}$
 $Key = \{A\}$

- R is not in BCNF
- Decomposition $R_1 = (A, B), R_2 = (B, C)$
 - R_1 and R_2 in BCNF
 - Lossless-join decomposition
 - Dependency preserving

Testing for BCNF

- To check if a non-trivial dependency α→β
 causes a violation of BCNF
 - 1. compute α^+ (the attribute closure of α), and
 - 2. verify that it includes all attributes of *R*, that is, it is a superkey of *R*.

Testing for BCNF

- Simplified test: To check if a relation schema R is in BCNF, it suffices to check only the dependencies in the given set F for violation of BCNF, rather than checking all dependencies in F⁺.
 - If none of the dependencies in F causes a violation of BCNF, then none of the dependencies in F⁺ will cause a violation of BCNF either.

Testing for BCNF

- However, simplified test using only F is incorrect when testing a relation in a decomposition of R
 - Consider R = (A, B, C, D, E), with F = { A → B, BC → D}
 - Decompose R into $R_1 = (A,B)$ and $R_2 = (A,C,D,E)$
 - Neither of the dependencies in F contain only attributes from
 (A,C,D,E) so we might be mislead into thinking R₂ satisfies BCNF.
 - In fact, dependency AC → D in F⁺ shows R₂ is not in BCNF.

Testing Decomposition for BCNF

- To check if a relation R_i in a decomposition of R is in BCNF,
 - Either test R_i for BCNF with respect to the restriction of F to R_i (that is, all FDs in F⁺ that contain only attributes from R_i)
 - or use the original set of dependencies F that hold on R, but with the following test:
 - for every set of attributes $\alpha \subseteq R_i$, check that α^+ (the attribute closure of α) either includes no attribute of R_i α , or includes all attributes of R_i .
 - If the condition is violated by some $\alpha\square \to \beta$ in F, the dependency

$$\alpha \square \rightarrow (\alpha^+ - \alpha \square) \cap R_i$$

can be shown to hold on R_i , and R_i violates BCNF.

• We use above dependency to decompose R_i

Example of BCNF Decomposition

- R = (A, B, C) $F = \{A \rightarrow B \}$ $B \rightarrow C\}$ $Key = \{A\}$
- R is not in BCNF (B → C but B is not superkey)
- Decomposition
 - $-R_1 = (B, C)$ $-R_2 = (A,B)$

Example of BCNF Decomposition

- class (course_id, title, dept_name, credits, sec_id, semester, year, building, room_number, capacity, time_slot_id)
- Functional dependencies:
 - course_id→ title, dept_name, credits
 - building, room_number→capacity
 - course_id, sec_id, semester, year→building, room_number, time_slot_id

Example of BCNF Decomposition

- A candidate key {course_id, sec_id, semester, year}.
- BCNF Decomposition:
 - course_id→ title, dept_name, credits holds
 - but course_id is not a superkey.
 - We replace *class* by:
 - course(course_id, title, dept_name, credits)
 - class-1 (course_id, sec_id, semester, year, building, room number, capacity, time slot id)

BCNF Decomposition

- course is in BCNF
 - How do we know this?
- building, room_number→capacity holds on class-1
 - but {building, room_number} is not a superkey for class-1.
 - We replace *class-1* by:
 - classroom (building, room_number, capacity)
 - section (course_id, sec_id, semester, year, building, room_number, time_slot_id)
- classroom and section are in BCNF.

BCNF and Dependency Preservation

It is not always possible to get a BCNF decomposition that is dependency preserving

•
$$R = (J, K, L)$$

 $F = \{JK \rightarrow L$
 $L \rightarrow K\}$

Two candidate keys = JK and JL

- R is not in BCNF
- Any decomposition of R will fail to preserve

$$JK \rightarrow L$$

This implies that testing for $JK \rightarrow L$ requires a join

Design Goals

- Goal for a relational database design is:
 - BCNF.
 - Lossless join.
 - Dependency preservation.
- If we cannot achieve this, we accept one of
 - Lack of dependency preservation
 - Redundancy due to use of 3NF

Design Goals

- Interestingly, SQL does not provide a direct way of specifying functional dependencies other than superkeys.
 - Can specify FDs using assertions, but they are expensive to test, (and currently not supported by any of the widely used databases!)
- Even if we had a dependency preserving decomposition, using SQL we would not be able to efficiently test a functional dependency whose left hand side is not a key.

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Overall Database Design Process

- We have assumed schema R is given
 - R could have been generated when converting
 E-R diagram to a set of tables.
 - R could have been a single relation containing all attributes that are of interest (called universal relation).
 - Normalization breaks R into smaller relations.
 - R could have been the result of some ad hoc design of relations, which we then test/convert to normal form.

ER Model and Normalization

- When an E-R diagram is carefully designed, identifying all entities correctly, the tables generated from the E-R diagram should not need further normalization.
- However, in a real (imperfect) design, there can be functional dependencies from non-key attributes of an entity to other attributes of the entity
 - Example: an employee entity with attributes
 department_name and building,
 and a functional dependency
 department_name → building
 - Good design would have made department an entity
- Functional dependencies from non-key attributes of a relationship set possible, but rare --- most relationships are binary

Denormalization for Performance

- May want to use non-normalized schema for performance
- For example, displaying prereqs along with course_id, and title requires join of course with prereq
- Alternative 1: Use denormalized relation containing attributes of course as well as prereq with all above attributes
 - faster lookup
 - extra space and extra execution time for updates
 - extra coding work for programmer and possibility of error in extra code
- Alternative 2: use a materialized view defined as course prereq
 - Benefits and drawbacks same as above, except no extra coding work for programmer and avoids possible errors

Other Design Issues

- Some aspects of database design are not caught by normalization
- Examples of bad database design, to be avoided:
 Instead of earnings (company_id, year, amount), use
 - earnings_2004, earnings_2005, earnings_2006, etc., all on the schema (company_id, earnings).
 - Above are in BCNF, but make querying across years difficult and needs new table each year
 - company_year (company_id, earnings_2004, earnings_2005,

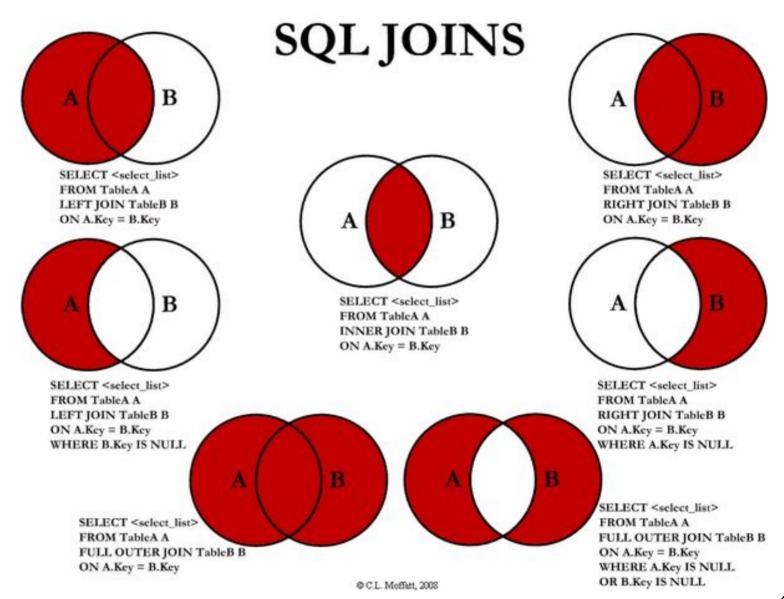
earnings_2006)

- Also in BCNF, but also makes querying across years difficult and requires new attribute each year.
- Is an example of a crosstab, where values for one attribute become column names
- Used in spreadsheets, and in data analysis tools

Lecture Outline

- Functional Dependencies Review
- BCNF Decomposition
- 3NF Decomposition
- Multivalued Decomposition
- Fourth Normal Form
- Database Design Process
- Midterm Review

Joins



- Join operations take two relations and return as a result another relation.
- A join operation is a Cartesian product which requires that tuples in the two relations match (under some condition).
 It also specifies the attributes that are present in the result of the join
- The join operations are typically used as subquery expressions in the from clause

Cartesian with where clause

Select name, course_id from instructor, teaches where instructor.ID = teaches.ID;

Natural Join

Select name, course_id from instructor natural join teaches;

- There is also join with using clause
 Select name, course_id
 from instructor join teaches using (ID);
- You must specify list of attributes to join upon
- Both relations must have the same name
- Similar to natural join except:
 - Not all attributes that are the same are joined upon

- There is also join with on condition
 - Select name, course_id
 - from instructor join teaches on (instructor.ID = teaches.ID);
- Arbitrary join condition
- Similar to using where clause to specify join condition
 - The on condition behaves differently for outer joins

select * from course, prereq where
course.course_id = prereq.course_id;

select * from course natural join prereq;

select * from course join prereq using(course_id);

select * from course join prereq on
course.course_id = prereq.course_id;

Outer Joins

- An extension of the join operation that avoids loss of information.
- Computes the join and then adds tuples from one relation that does not match tuples in the other relation to the result of the join.
- Uses null values.
- inner join join operations that do not preserve non-matched tuples

Left Outer Join

select * from course *natural* left outer join prereq;

Right Outer Join

select * from course *natural* right outer join prereq;

Full Outer Join

select * from course *natural* full outer join prereq;

A large organization has several parking lots which are used by staff.

Each parking lot has a unique name, location, capacity, and number of floors.

Each parking lot has parking spaces which are uniquely identified within that lot using a space number.

Each space is located on a particular floor within the lot.

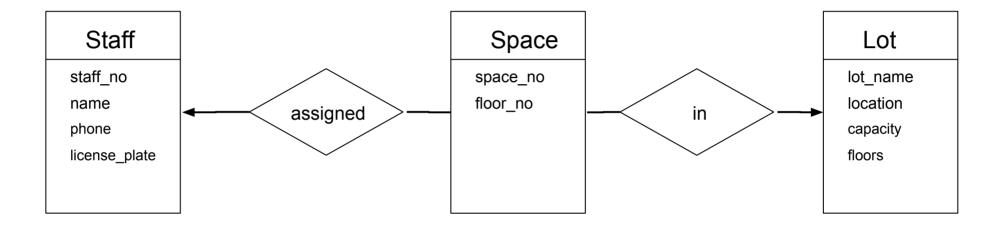
Members of staff are assigned the use of a parking space.

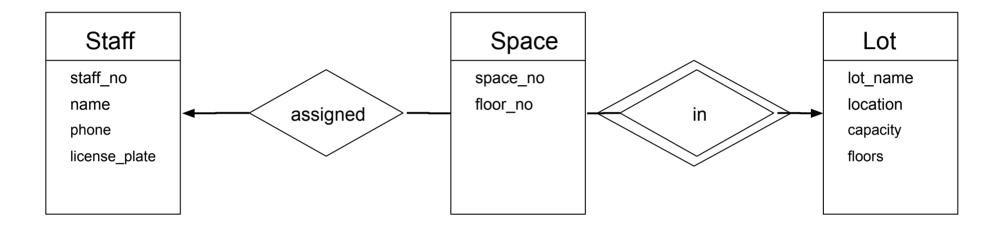
Each member of staff has a unique id number, name, telephone, and vehicle license plate number..

How should we begin?

How should we begin? Create an ER Diagram

What are the entity sets?
What are the relation sets?
Attributes?





Reduce to a relational model. Underline primary keys and use a + to indicate foreign keys.

```
Staff (<u>staff_no</u>, first_name, last_name, phone, license_plate)
Assignment(<u>staff_no(+), lot_name(+),</u>
space_number(+))
Space (<u>lot_name(+), space_number,</u>
floor_number)
Lot (<u>lot_name</u>, location, capacity, floors)
```

List the set of functional dependencies for each relation in your model that originated from the problem statement above. For each functional dependency, use the form $\alpha \to \beta$ where α and β are one or more attributes from your relation schema.

Indicate the relation and the set of functional dependencies using this pattern:

Relation name: $F = \{a \rightarrow b, c \rightarrow d\}$

```
Staff:
```

```
F = { staff_no→ first_name, last_name, phone, license_plate}
```

Assignment:

```
F = { staff_no, lot_name → space_number}
```

Space:

```
F = \{ lot_name, space_number \rightarrow floor_number \}
```

Lot:

```
F = { lot_name → location, capacity, floors }
```

Do we pass the test for BCNF?

Why or why not?

Do we pass the test for BCNF?

Yes, because they are all non-trivial and all superkeys.

Based on the functional dependencies from above, use Armstrong's Axioms and their derivatives, to derive three new functional dependencies.

DECOMPOSITION

```
lot_name → location, capacity, floors
lot_name → location, capacity
lot_name → floors
```

REFLEXIVITY

```
staff_no→ staff_no
```

AUGMENTATION

```
staff_no→ license_plate
staff_no, phone → license_plate, phone
```